

آزمایشگاه مکانیک خاک





Karl Terzaghi
1883-1963



C.A. Coulomb
1736-1806



WJM Rankine
1820-1872



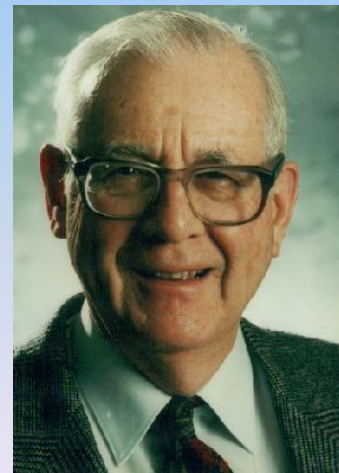
A. Casagrande
1902-1981



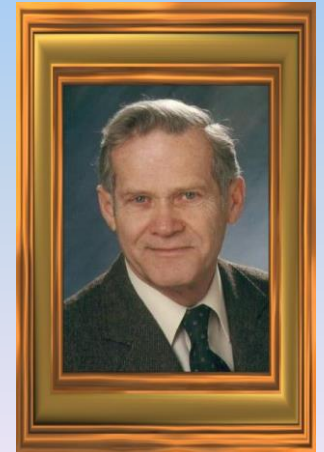
L. Bjerrum
1918-1973



A.W. Skempton
1914-



G.F. Sowers
1921-1996



G.A. Leonards
1921-1997

SOIL ELEMENTS

Degree of Saturation in %

$$S = V_w / V_v$$

Voids Ratio

$$e = V_v / V_s$$

Porosity in %

$$n = V_v / V_t$$

Water

Content in %

$$w = W_w / W_s$$

Bulk density

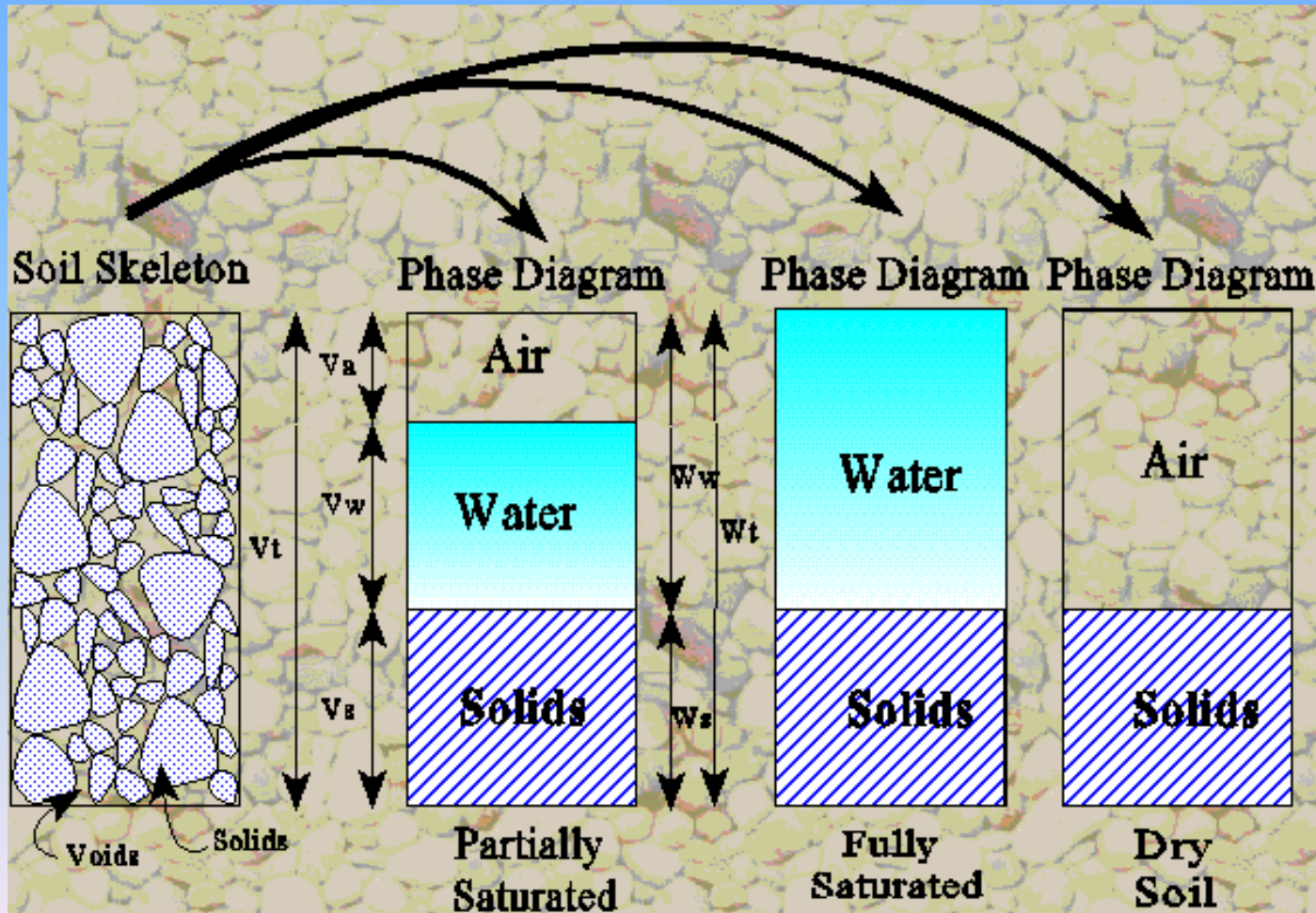
gm/cc

$$\gamma = W / V_t$$

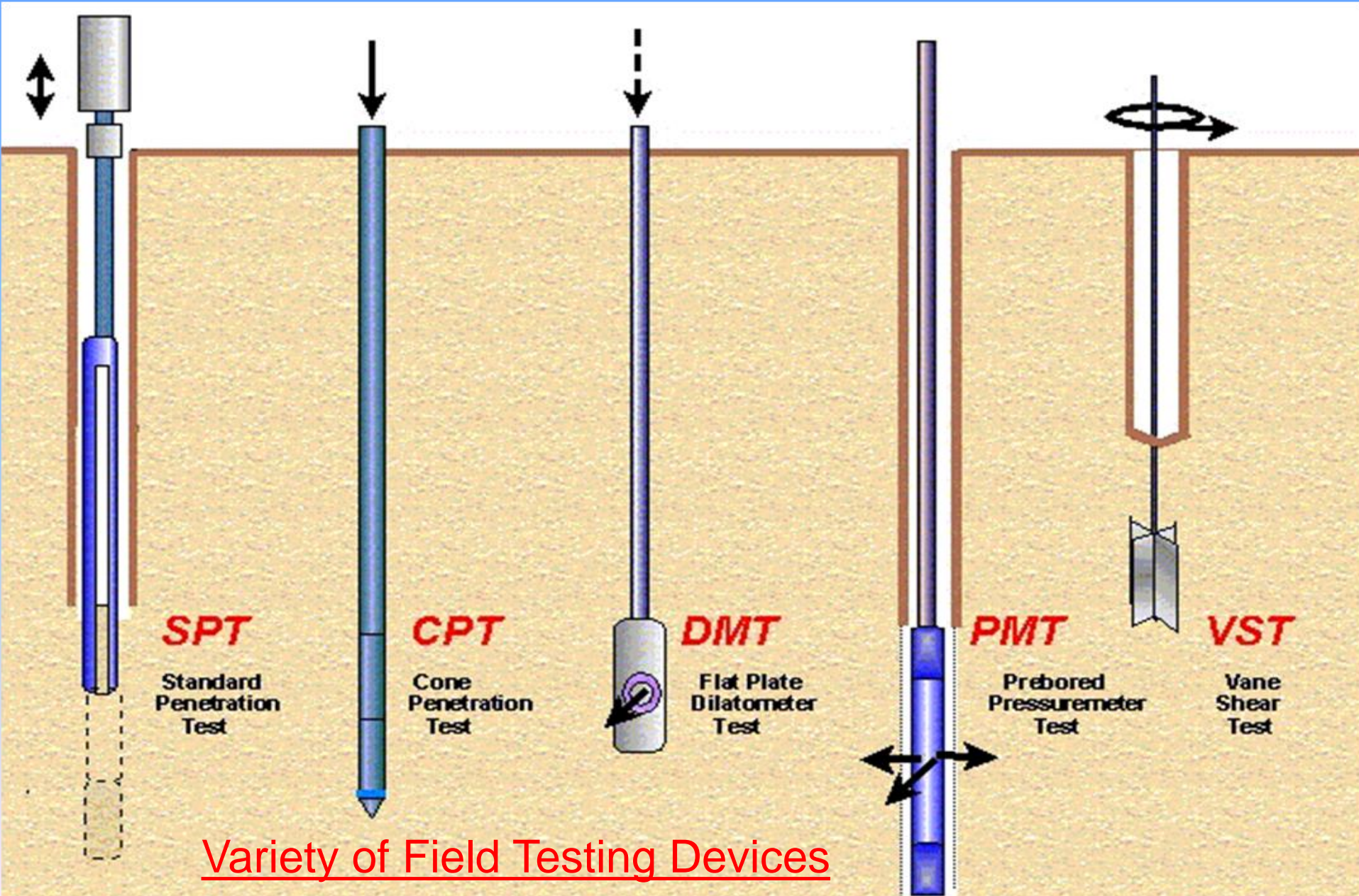
Dry density

gm/cc

$$\gamma_d = W_s / V_t$$



Soil Testing

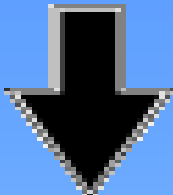


آزمایش نفوذ استاندارد SPT

Standard penetration test

- 1-Using a 140 lb. (64 kg) driving mass falling free from a height of 30 in. (762 mm)...
- 2-Driving the standard split spoon sampler a distance of 18 in. (457 mm) into the soil, and...
- 3-Counting the number of blows (N) to drive the sampler 12 in. (6 in. plus 6 in.) [152 mm plus 152 mm].





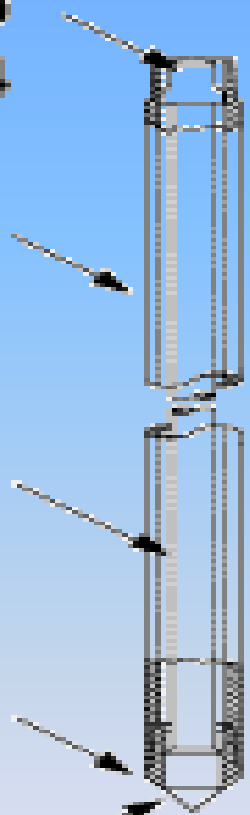
**Centering
Drive Cap
16914**

**Probe Rod
3.25 in.**

**Probe Rod
1.5 in.**

**Cutting Shoe, SPT
20737**

**Solid Drive Tip, SPT
21114**



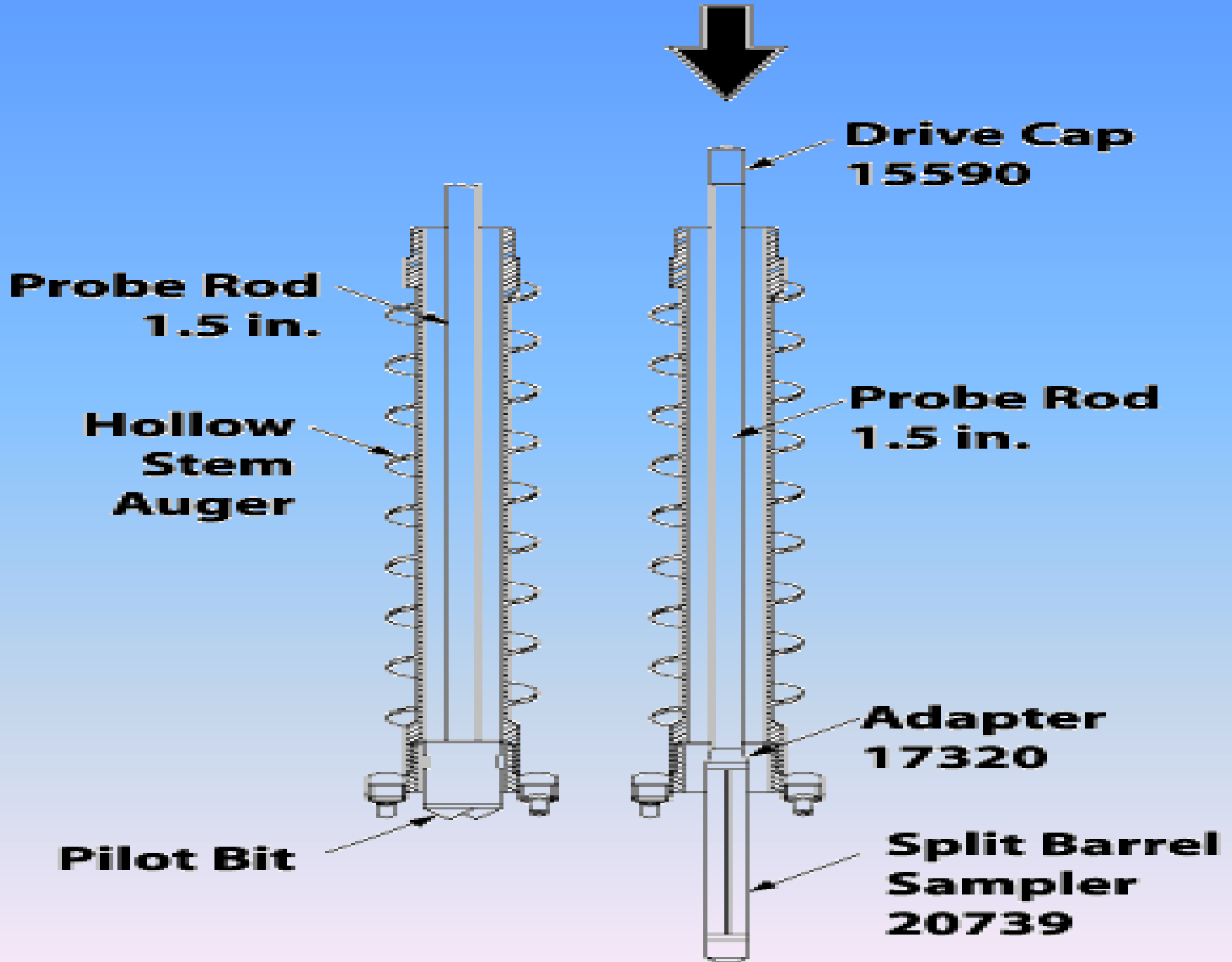
**Drive Cap
15590**

**Probe Rod
1.5 in.**

**Adapter
17320**

**Split Barrel
Sampler
20739**











Moisture Content

- The moisture content, m , is defined as

$$m = \frac{\textit{Weight of Water}}{\textit{Weight of Solids}} = \frac{W_w}{W_s}$$

In terms of e , S , G_s and γ_w

$$W_w = \gamma_w V_w = \gamma_w e S V_s$$

$$W_s = \gamma_s V_s = \gamma_w G_s V_s$$

hence

$$m = \frac{e S}{G_s}$$

Example 1

- Distribution by mass and weight

| Phase | Trimmings Mass (g) | Sample Mass, M (g) | Sample Weight, Mg (kN) |
|-------|-----------------------|-----------------------|---------------------------|
| Total | 55 | 290 | 2845×10^{-6} |
| Solid | 45 | 237.3 | 2327.9×10^{-6} |
| Water | 10 | 52.7 | 517×10^{-6} |

- Distribution by volume (assume $G_s = 2.65$)

Total Volume $V = \pi r^2 l$

Water Volume $V_w = \frac{W_w}{\gamma_w}$

Solids Volume $V_s = \frac{W_s}{\gamma_w G_s}$

Air Volume $V_a = V - V_s - V_w$

Moisture content $m = \frac{W_w}{W_s} = \frac{10}{45} = 0.222 = 22.2\%$

Voids ratio $e = \frac{V_v}{V_s} = \frac{V_a + V_w}{V_s} = 0.755$

Degree of Saturation $S = \frac{V_w}{V_v} = \frac{V_w}{V_a + V_w} = 0.780 = 78.0\%$

Bulk unit weight $\gamma_{bulk} = \frac{W}{V} = 18.1 \text{ kN} / \text{m}^3$

Dry unit weight $\gamma_{dry} = \frac{W_s}{V} = 14.8 \text{ kN} / \text{m}^3$

Saturated unit weight $\gamma_{sat} = \frac{(W + 14.9 \times 10^{-6} \times 9.81)}{V} = 19.04 \text{ kN} / \text{m}^3$

Note that $\gamma_{dry} < \gamma_{bulk} < \gamma_{sat}$

Atterberg Limits

- ▶ Particle size is not that useful for fine grained soils

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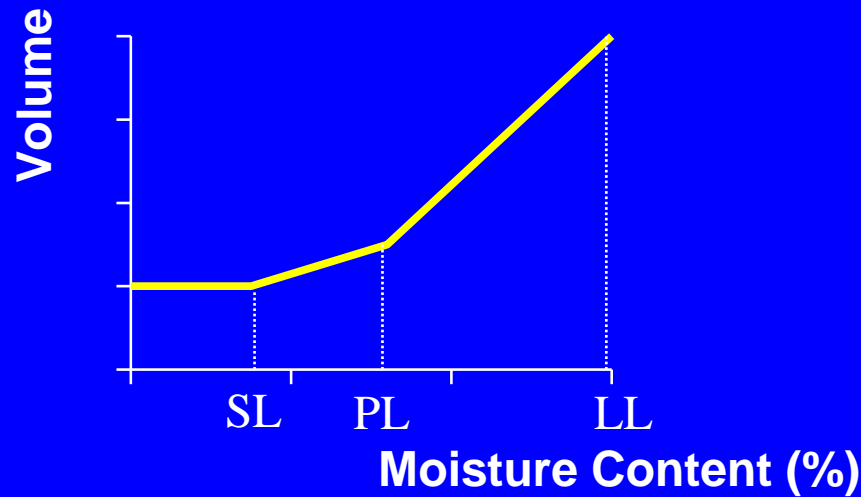


Figure 4 Moisture content versus volume relation during drying

Atterberg Limits

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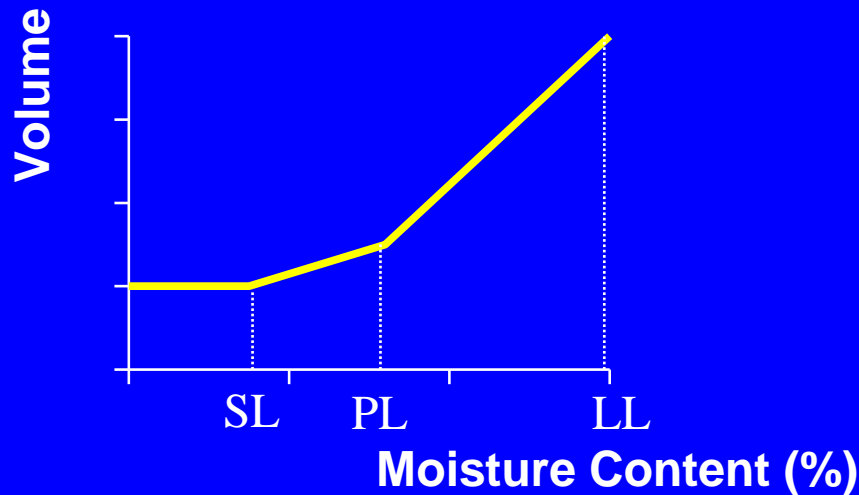


Figure 4 Moisture content versus volume relation during drying

- ▶ SL - Shrinkage Limit
- ▶ PL - Plastic Limit
- ▶ LL - Liquid limit

Atterberg Limits

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$$\text{Plasticity Index} = \text{LL} - \text{PL} = \text{PI} \text{ or } I_p$$

Atterberg Limits

SL - Shrinkage Limit

PL - Plastic Limit

LL - Liquid limit

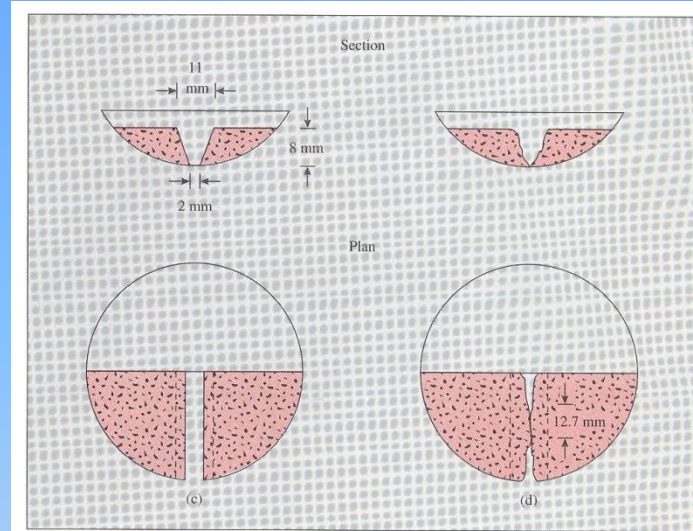
$$\text{Moisture content} = \frac{\text{mass of water}}{\text{mass of solids}}$$

$$\text{Plasticity Index} = \text{LL} - \text{PL} = \text{PI or } I_p$$

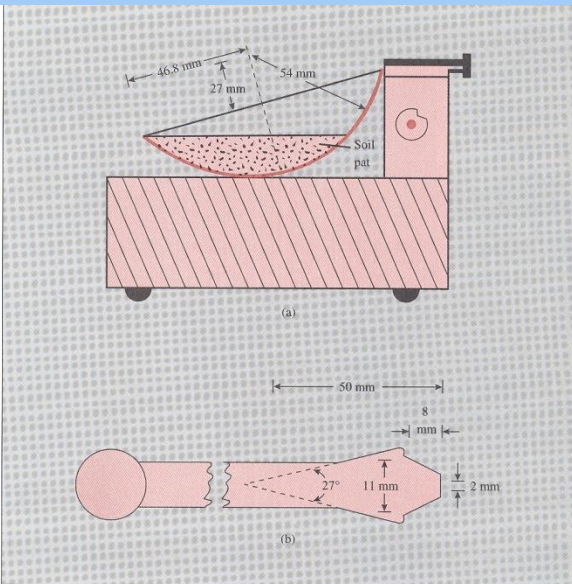
$$\text{Liquidity Index} = (m - \text{PL})/I_p = \text{LI}$$

LIQUID LIMIT - ATTERBERG'S LIMITS

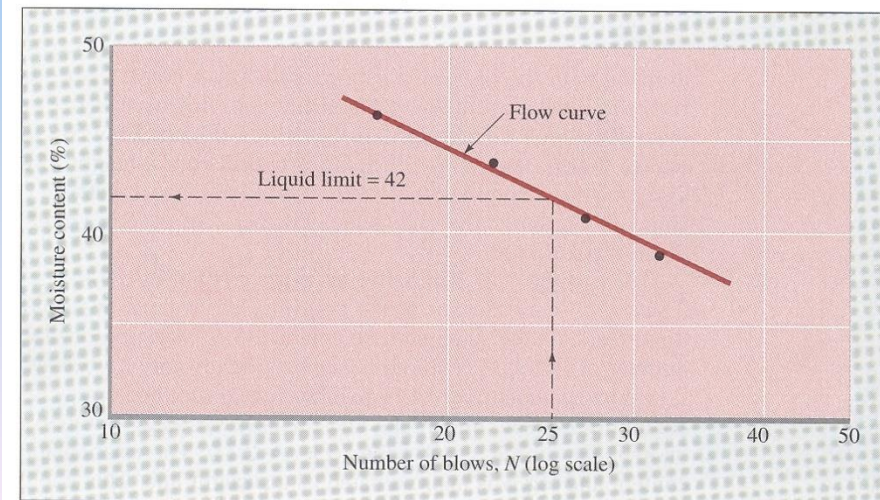
Liquid Limit is the water content at which 25 blows cause the groove to close.



▼ FIGURE 2.9 (Continued)



▼ FIGURE 2.9 Liquid limit test: (a) liquid limit device; (b) grooving tool; (c) soil pat before test; (d) soil pat after test



▼ FIGURE 2.11 Flow curve for liquid limit determination of a clayey silt

PLASTIC & SHRINKAGE LIMIT

Plastic Limit is water content at which 3 mm diameter roller of soil starts crumbling

Shrinkage Limit is water content beyond reduction which does not cause volume decrease

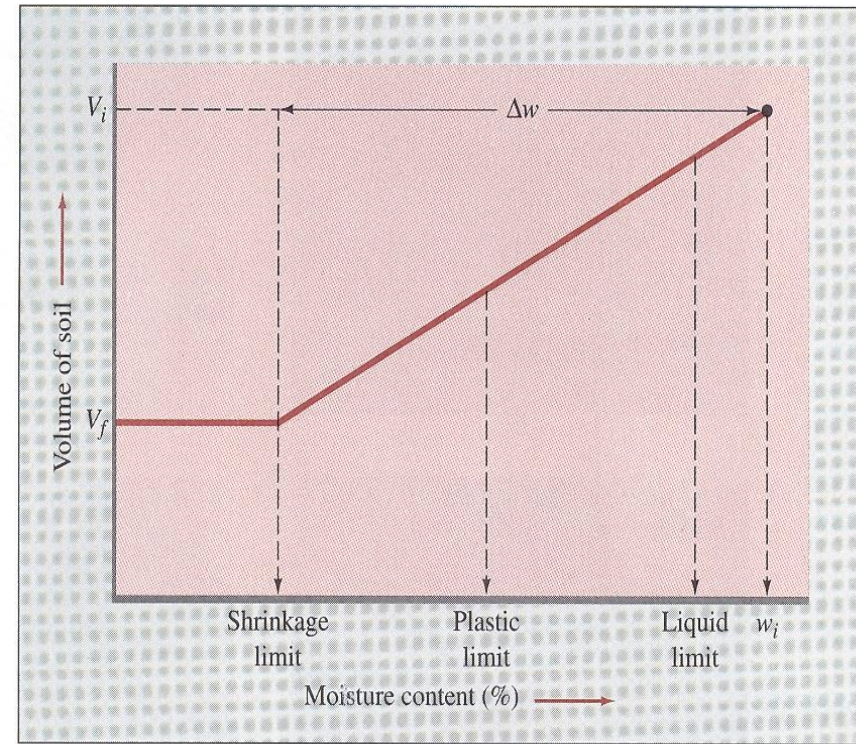
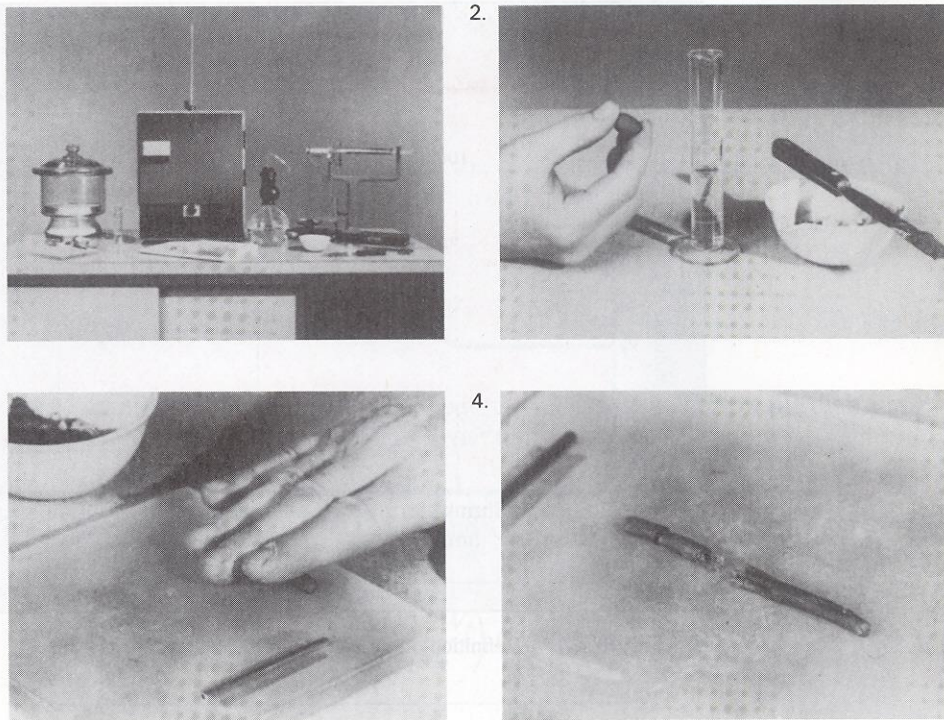
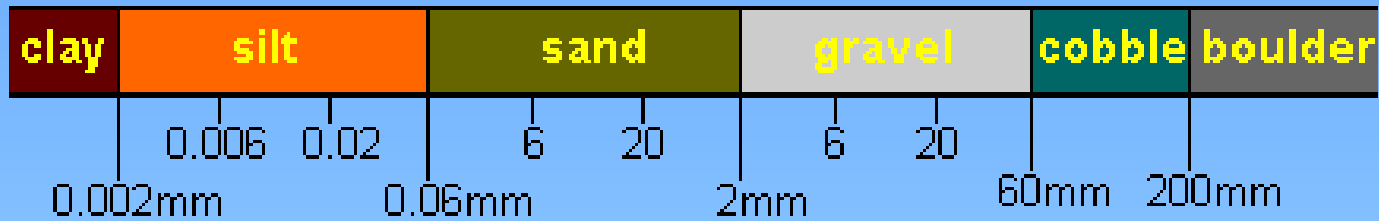


FIGURE 2.12 Plastic limit test: (1) equipment; (2) beginning of test; (3) thread being rolled; (4)

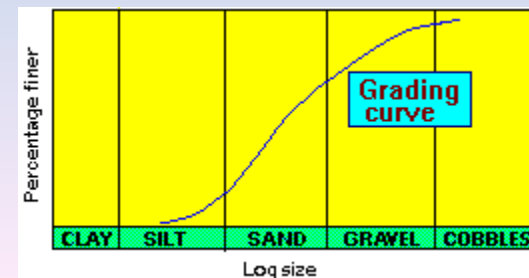
Plasticity Index I_P or $I_P = \text{Liquid Limit (LL or } W_L) - \text{Plastic Limit (PL or } W_P)$

– Plastic Limit (PL or W_P)

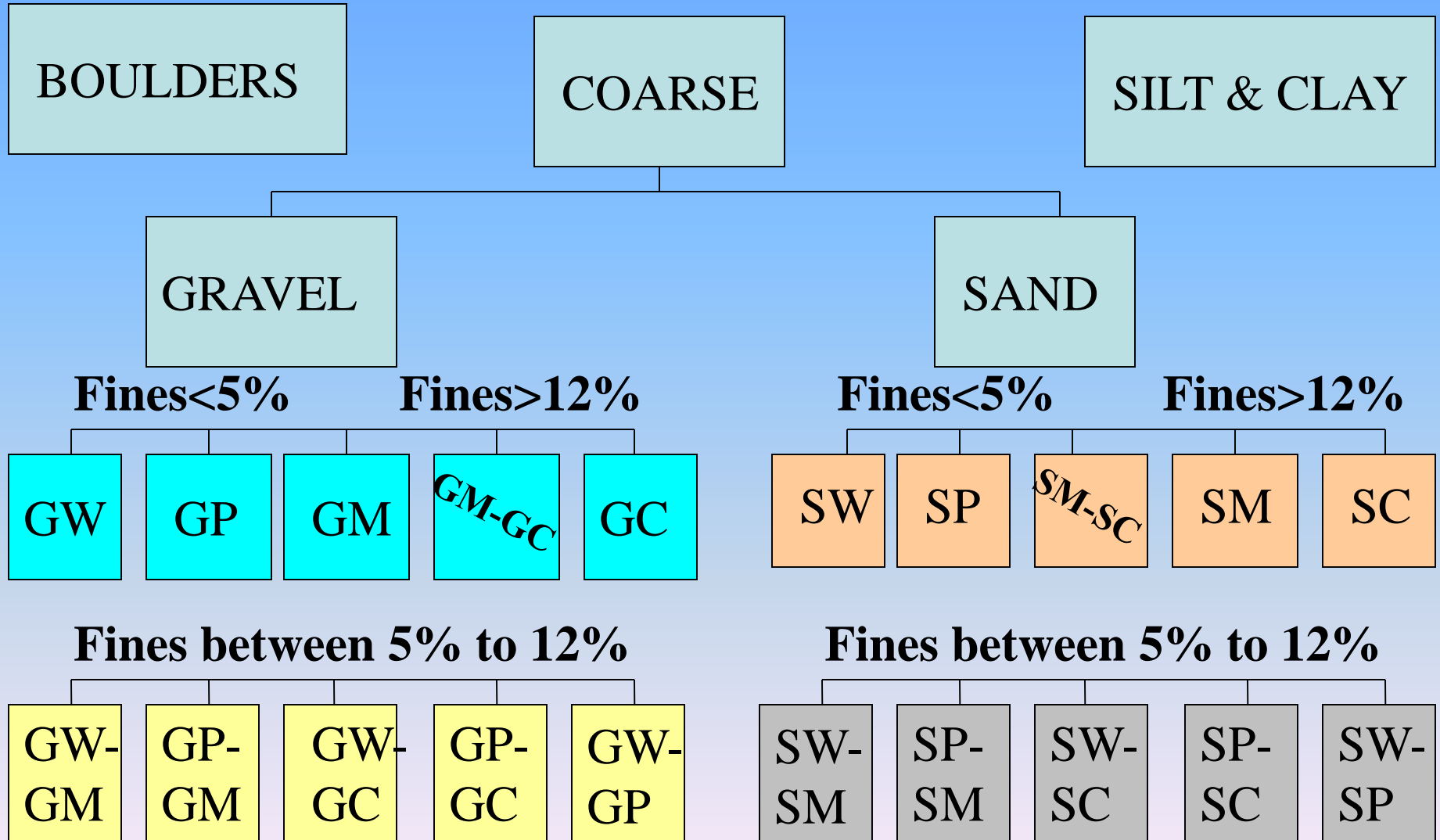
Aggregates (سنگدانه ها)



| | | | |
|-------------------|-------------|--------|------------------|
| Very coarse soils | BOULDERS | | > 200 mm |
| | COBBLES | | 60 - 200 mm |
| Coarse soils | G GRAVEL | coarse | 20 - 60 mm |
| | | medium | 6 - 20 mm |
| | | fine | 2 - 6 mm |
| | S SAND | coarse | 0.6 - 2.0 mm |
| | | medium | 0.2 - 0.6 mm |
| | | fine | 0.06 - 0.2 mm |
| Fine soils | M SILT | coarse | 0.02 - 0.06 mm |
| | | medium | 0.006 - 0.02 mm |
| | | fine | 0.002 - 0.006 mm |
| | C CLAY | | < 0.002 mm |



CLASSIFICATION IS:1498 - 1970



Sieve analysis

(Grading)

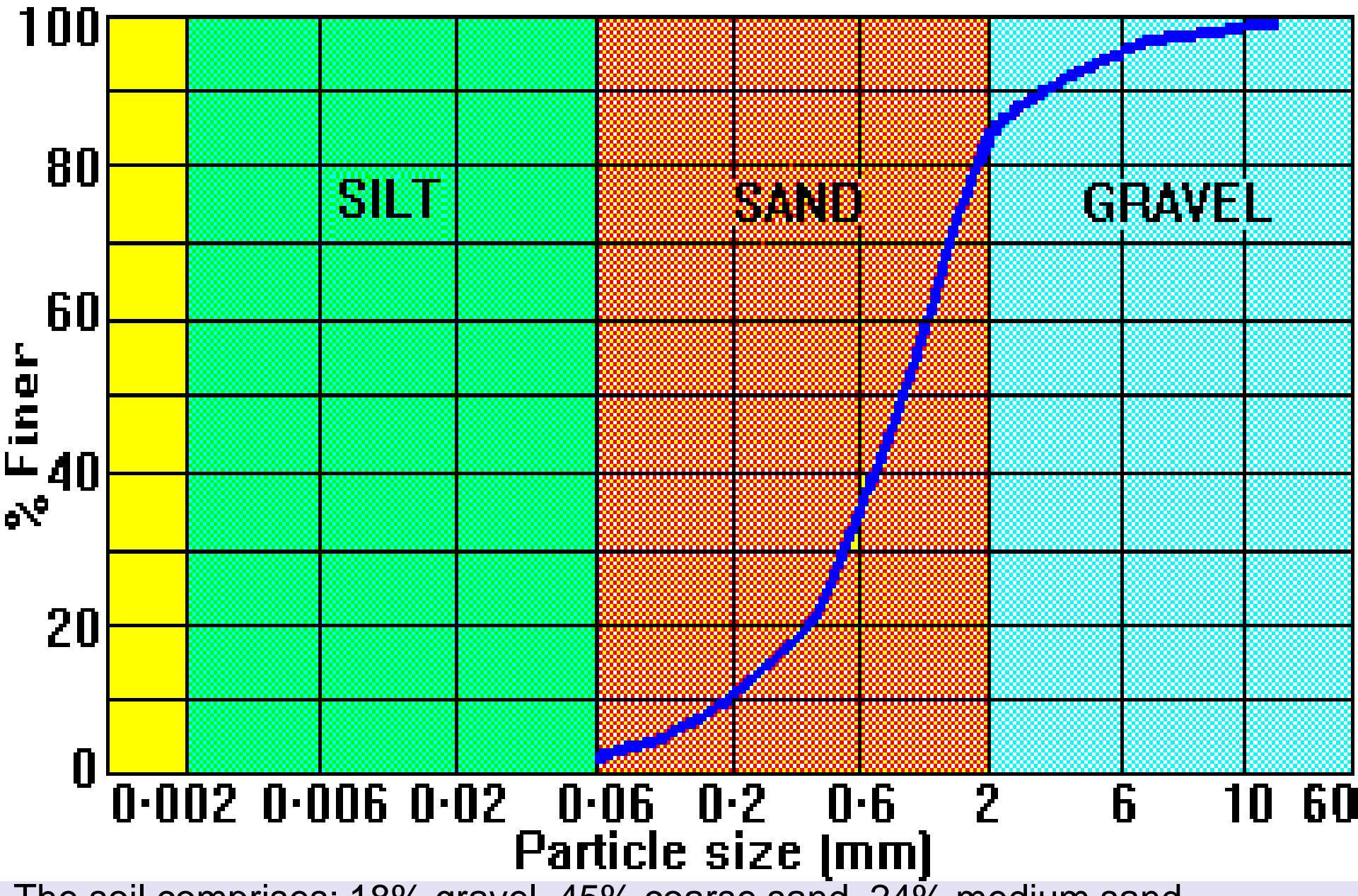


Sieve Analysis Apparatus: A) Sieve aperture sizes, B) Dry oven, C) Sieve shaker, D) Mortar & Tray, E) Rubber pestle, [F] Balance

Sieve analysis example

The results of a dry-sieving test are given below, together with the grading analysis and grading curve. Note carefully how the tabulated results are set out and calculated. The grading curve has been plotted on special semi-logarithmic paper; you can also do this analysis using a spreadsheet.

| Sieve mesh size (mm) | Mass retained (g) | Percentage retained | Percentage finer (passing) |
|----------------------|-------------------|---------------------|----------------------------|
| 14.0 | 0 | 0 | 100.0 |
| 10.0 | 3.5 | 1.2 | 98.8 |
| 6.3 | 7.6 | 2.6 | 86.2 |
| 5.0 | 7.0 | 2.4 | 93.8 |
| 3.35 | 14.3 | 4.9 | 88.9 |
| 2.0 | 21.1 | 7.2 | 81.7 |
| 1.18 | 56.7 | 19.4 | 62.3 |
| 0.600 | 73.4 | 25.1 | 37.2 |
| 0.425 | 22.2 | 7.6 | 29.6 |
| 0.300 | 26.9 | 9.2 | 20.4 |
| 0.212 | 18.4 | 6.3 | 14.1 |
| 0.150 | 15.2 | 5.2 | 8.9 |
| 0.063 | 17.5 | 6.0 | 2.9 |
| Pan | 8.5 | 2.9 | |
| TOTAL | 292.3 | 100.0 | |



The soil comprises: 18% gravel, 45% coarse sand, 24% medium sand, 10% fine sand, 3% silt, and is classified therefore as: a **well-graded gravelly SAND**

By Method 1:

| Sieve Sizes (mm) | Mass Retained (g) | Percentage Retained (g) | Percentage Passing (%) |
|------------------|-------------------|---------------------------------------|------------------------|
| 1.18 | 0 | 0 | 100 |
| 0.600 | 20 | $(20/500) \times 100 = 4$ | $100 - 4 = 96$ |
| 0.300 | 170 | $(170/500) \times 100 = 34$ | $96 - 34 = 62$ |
| 0.150 | 235 | $(235/500) \times 100 = 47$ | $62 - 47 = 15$ |
| 0.063 | 71 | $(71/500) \times 100 = 14.2$ | $15 - 14.2 = 0.8$ |
| Pan | 3.5 | Check: $(3.5/500) \times 100 = 0.7\%$ | |

By Method 2:

| Sieve Sizes (mm) | Mass Retained (g) | Cumulative Mass Passing (g) | Percentage Passing (%) |
|------------------|-------------------|-----------------------------|------------------------------|
| 1.18 | 0 | $500 - 0 = 500$ | 100 |
| 0.600 | 20 | $500 - 20 = 480$ | $(480/500) \times 100 = 96$ |
| 0.300 | 170 | $480 - 170 = 310$ | $(310/500) \times 100 = 62$ |
| 0.150 | 235 | $310 - 235 = 75$ | $(75/500) \times 100 = 15$ |
| 0.063 | 71 | $75 - 71 = 4$ | $(4/500) \times 100 = 0.8$ |
| Pan | 3.5 | $4 - 3.5 = 0.5$ | $(0.5/500) \times 100 = 0.1$ |

Calculation Formula:

Weight of dried soil sample (initial sample mass), $W_{\text{total}} = 500 \text{ g}$

Percentage Retained = $(\text{Mass Retained} / W_{\text{total}}) \times 100 \%$

| Sieve Opening (mm) | Mass of Soil Retained, M_n | Percent of Mass Retained, R_n | Cumulative Percent Retained, $\sum R_n$ | Percent Finer, $100 - \sum R_n$ (%) |
|--------------------|------------------------------|---------------------------------|---|-------------------------------------|
| 4.75 | 154 | $(154/822) \times 100 = 18.7$ | 18.7 | $100 - 18.7 = 81.3$ |
| 2.36 | 72 | $(72/822) \times 100 = 8.7$ | $18.7 + 8.7 = 27.4$ | $100 - 27.4 = 72.6$ |
| 1.18 | 72 | $(72/822) \times 100 = 8.7$ | $27.4 + 8.7 = 36.1$ | $100 - 36.1 = 63.9$ |
| 0.60 | 141 | $(141/822) \times 100 = 17.1$ | $36.1 + 17.1 = 53.2$ | $100 - 53.2 = 46.8$ |
| 0.425 | 85 | $(85/822) \times 100 = 10.3$ | $53.2 + 10.3 = 63.5$ | $100 - 63.5 = 36.5$ |
| 0.30 | 80 | $(80/822) \times 100 = 9.7$ | $63.5 + 9.7 = 73.2$ | $100 - 73.2 = 26.8$ |
| 0.15 | 149 | $(149/822) \times 100 = 18.1$ | $73.2 + 18.1 = 91.3$ | $100 - 91.3 = 8.7$ |
| 0.075 | 45 | $(45/822) \times 100 = 5.5$ | $91.3 + 5.5 = 96.8$ | $100 - 96.8 = 3.2$ |
| Pan | 24 | $(24/822) \times 100 = 2.9$ | $96.8 + 2.9 = 99.7$ | - |

Calculation Formula:

Weight of dried soil sample, $W_{total} = 824 \text{ g}$

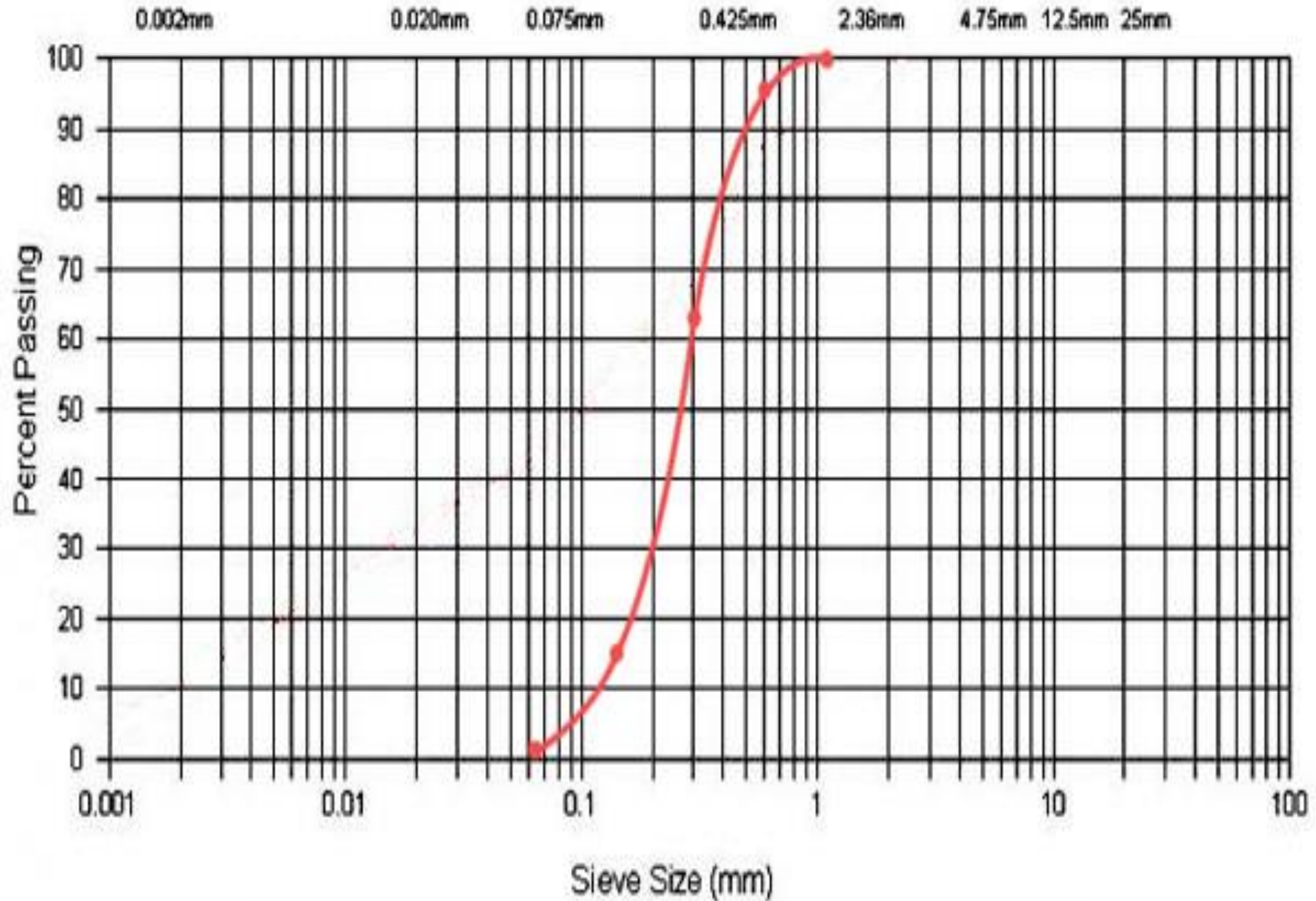
Percent of Mass Retained, $R_n = (M_n / W_1) \times 100 \%$

Total Mass of Soil Retained, $\sum M_n = W_1 = (154 + 72 + 72 + 141 + 85 + 80 + 149 + 45 + 24) = 822 \text{ g}$

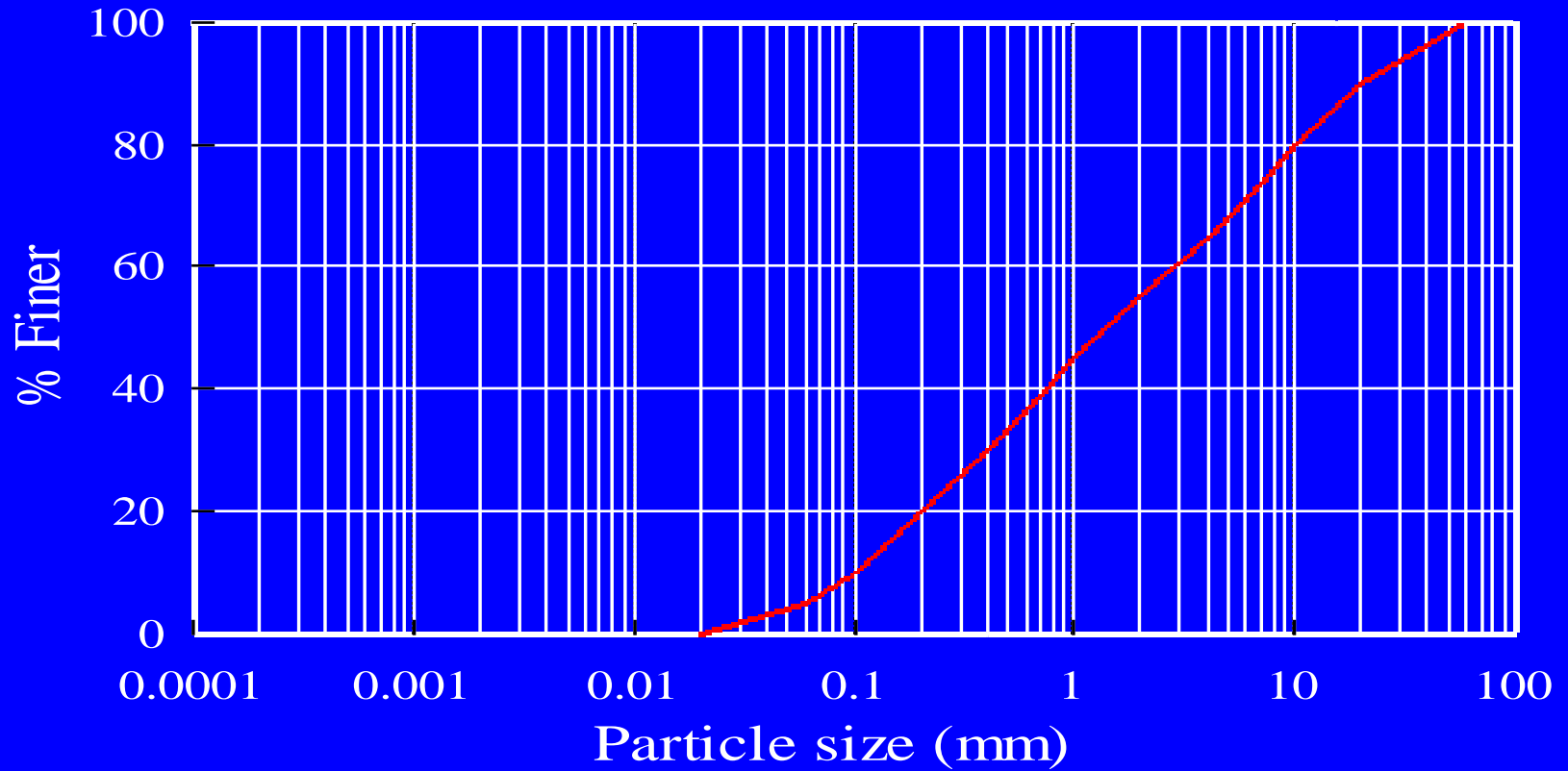
Mass Loss during Sieve Analysis; $[(W_{total} - W_1) / W_{total}] \times 100 \% = [(824 - 822) / 824] \times 100 = 0.2 \%$

Note: OK if $< 2 \%$

The Graphs



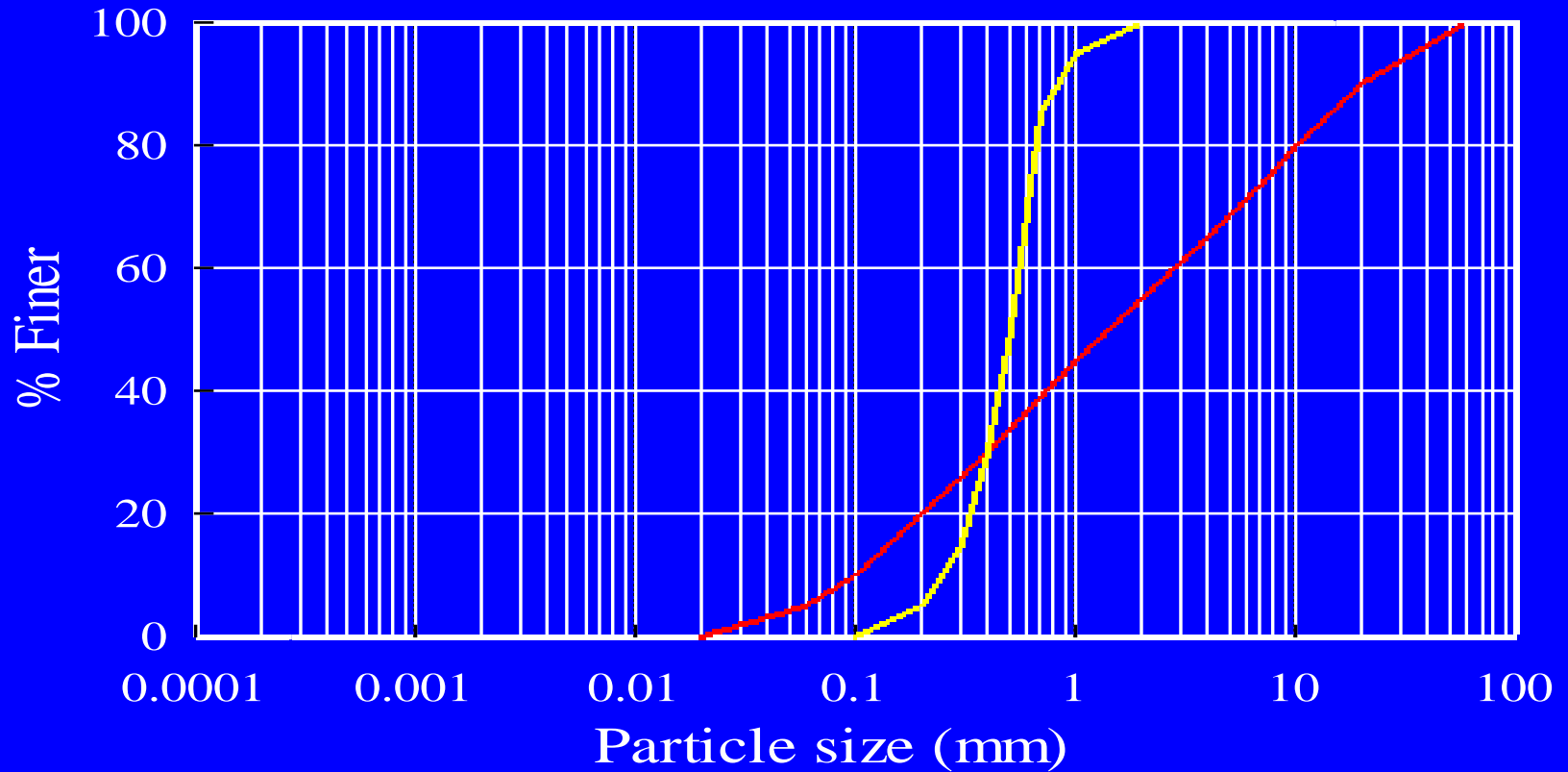
Grading curves



W

Well graded

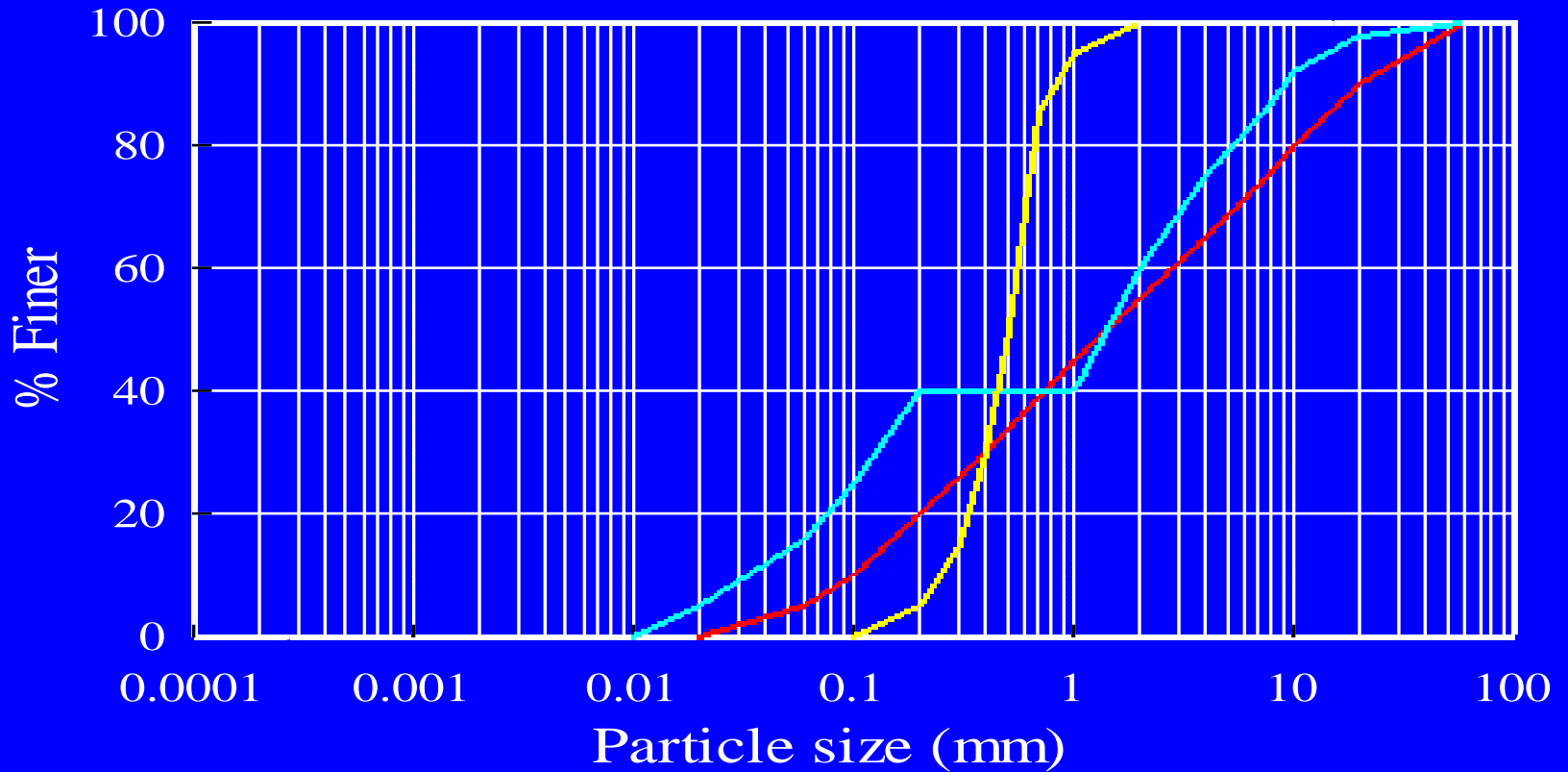
Grading curves



W Well graded

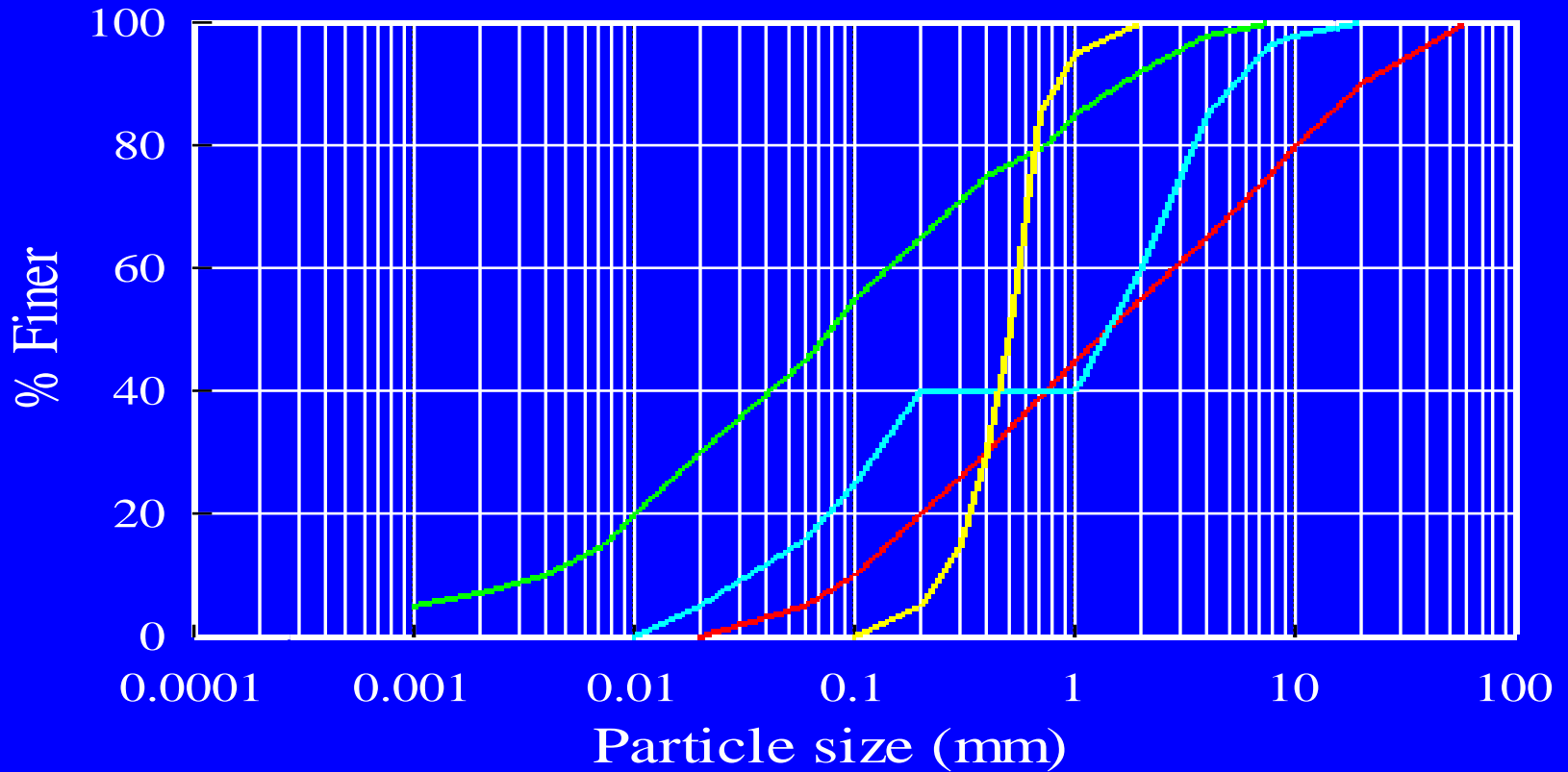
U Uniform

Grading curves



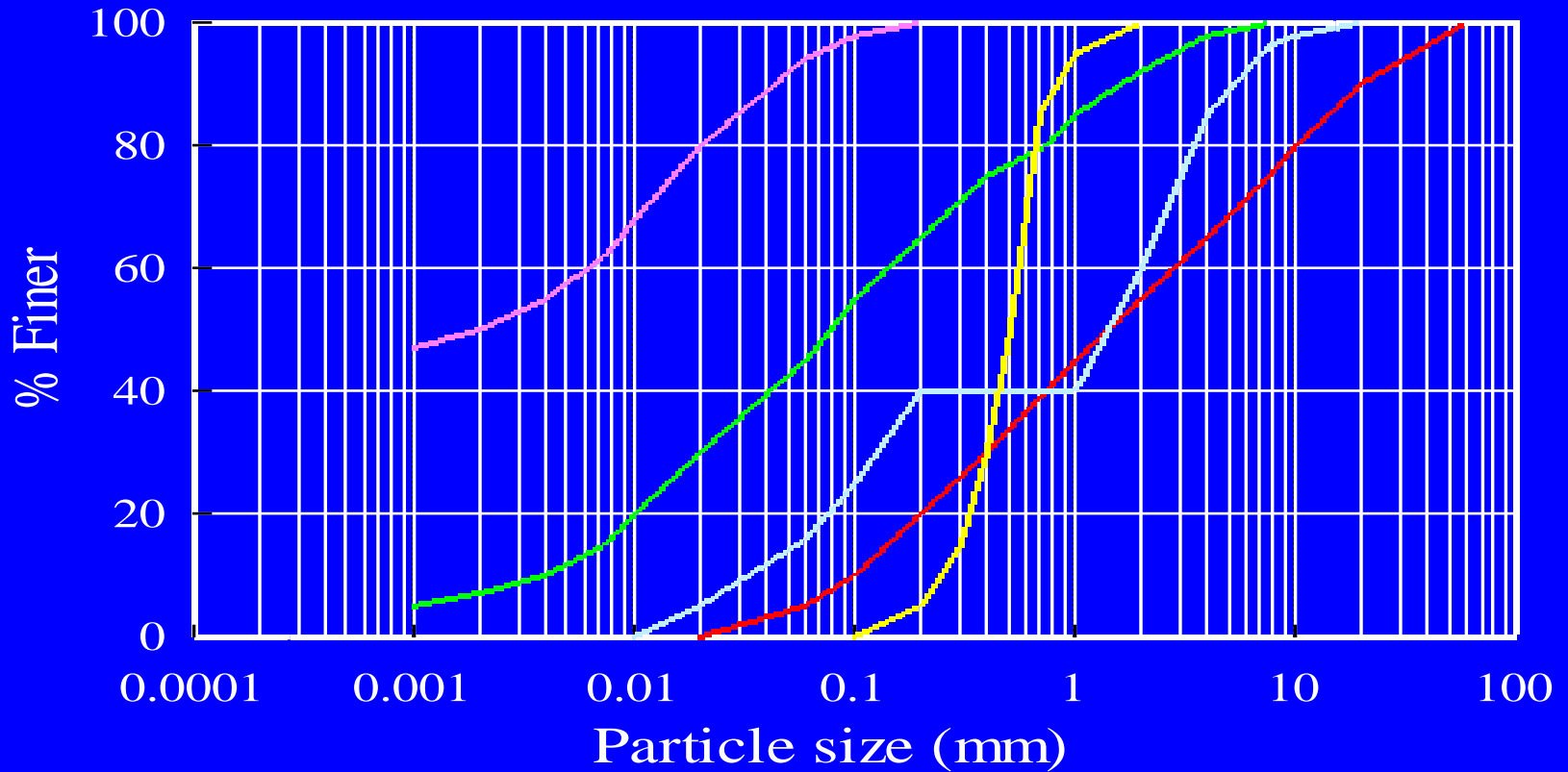
- W Well graded
- U Uniform
- P Poorly graded

Grading curves



- W Well graded
- U Uniform
- P Poorly graded
- C Well graded with some clay

Grading curves



- W Well graded
- U Uniform
- P Poorly graded
- C Well graded with some clay
- F Well graded with an excess of fines

Unified Soil Classification

To determine if W or P, calculate C_u and C_c

$$C_u = \frac{D_{60}}{D_{10}}$$

x% of the soil has particles smaller than D_x

$$C_c = \frac{D_{30}^2}{(D_{60} \times D_{10})}$$

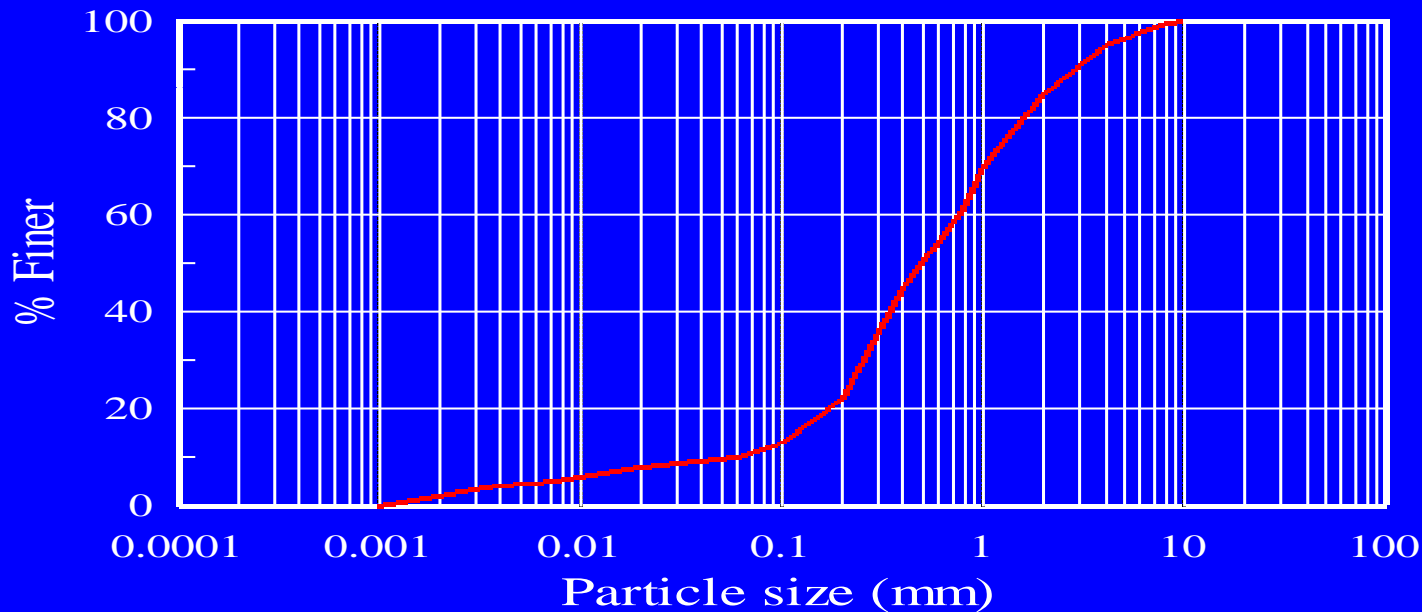
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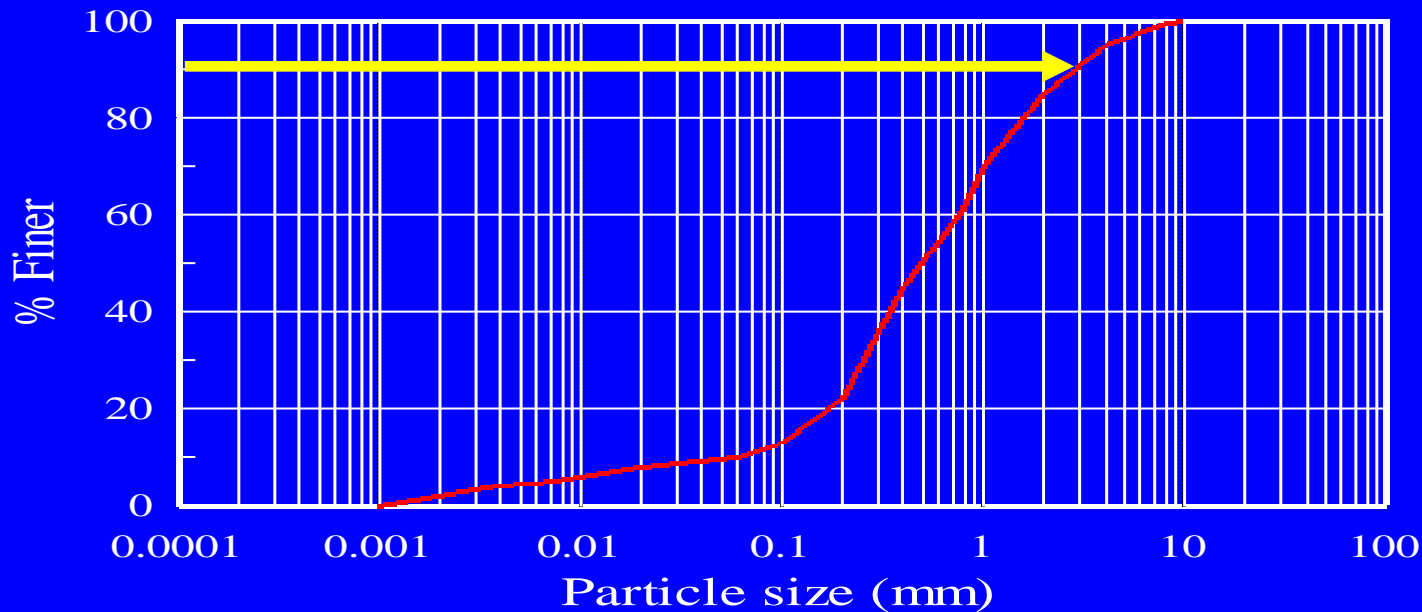
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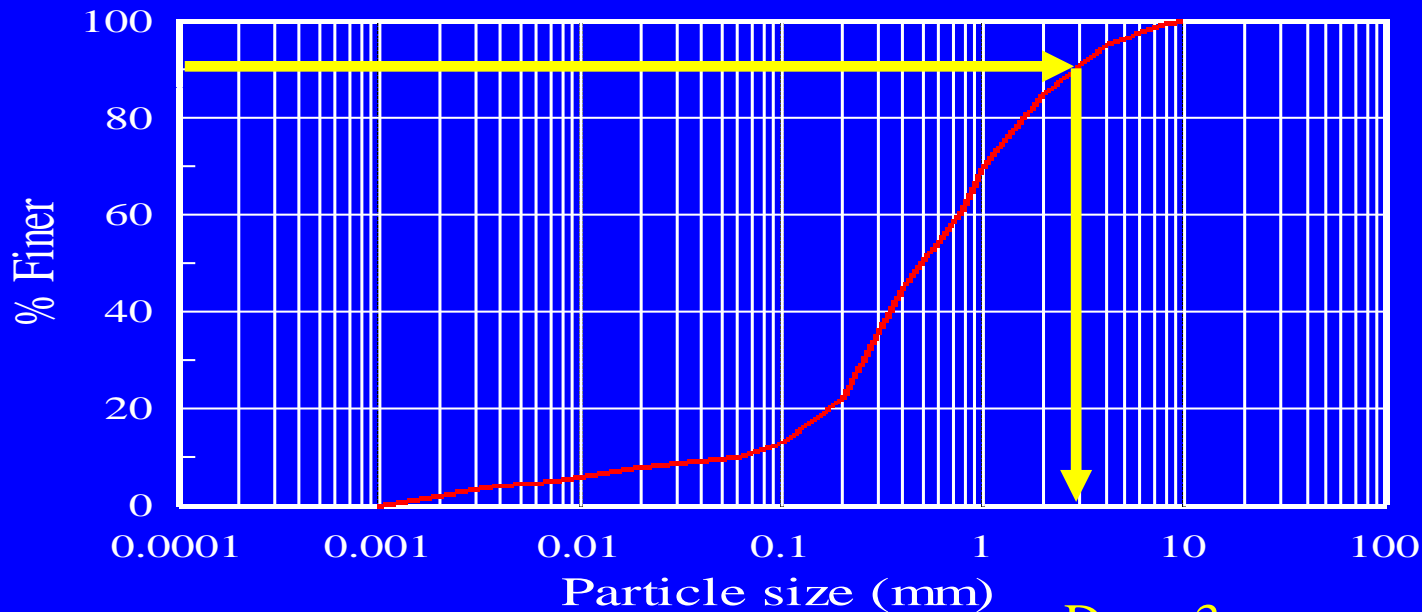
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x% of the soil has particles smaller than D_x



$D_{90} = 3$
mm

Unified Soil Classification

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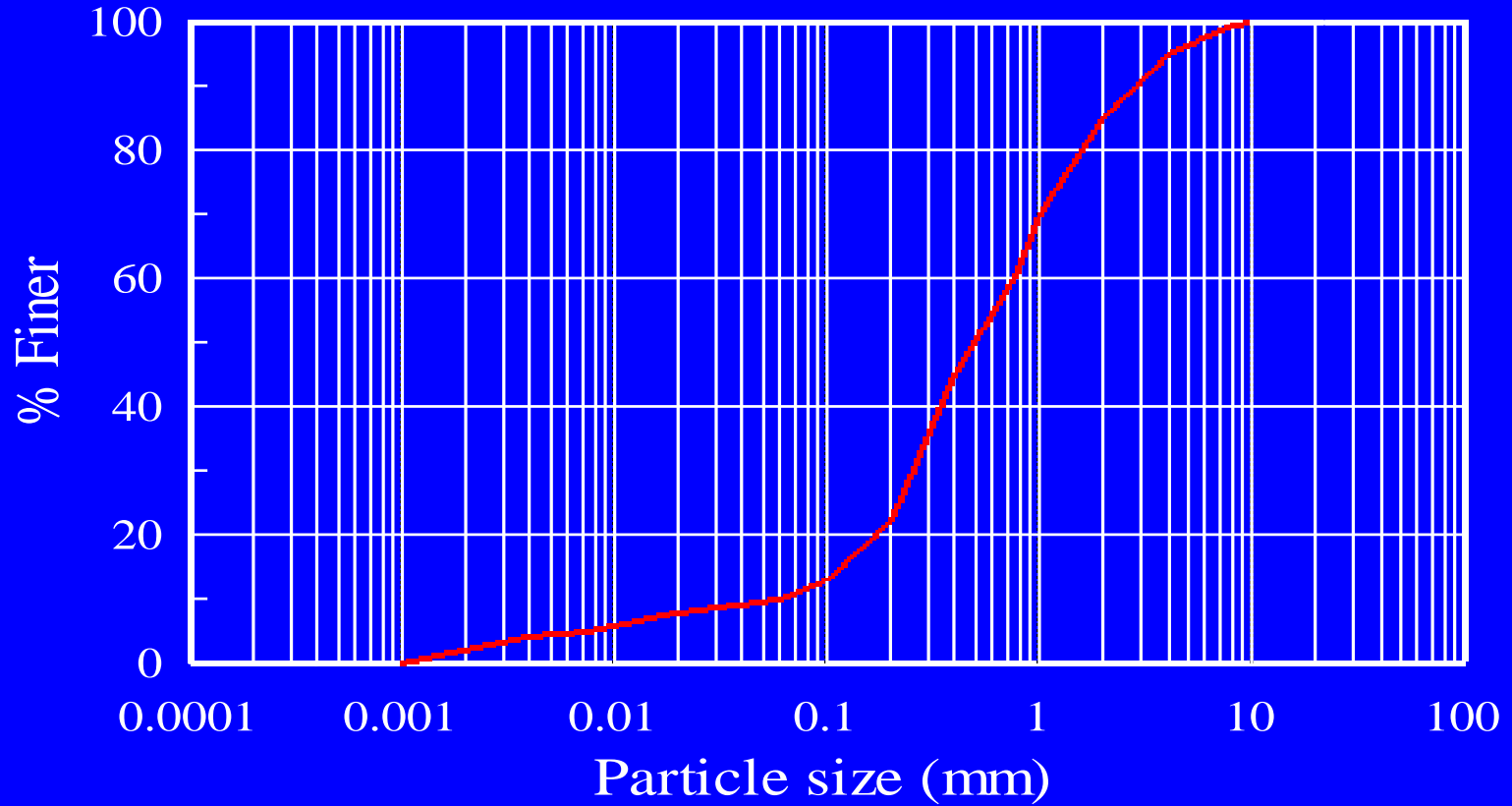
$$C_u = \frac{D_{60}}{D_{10}}$$

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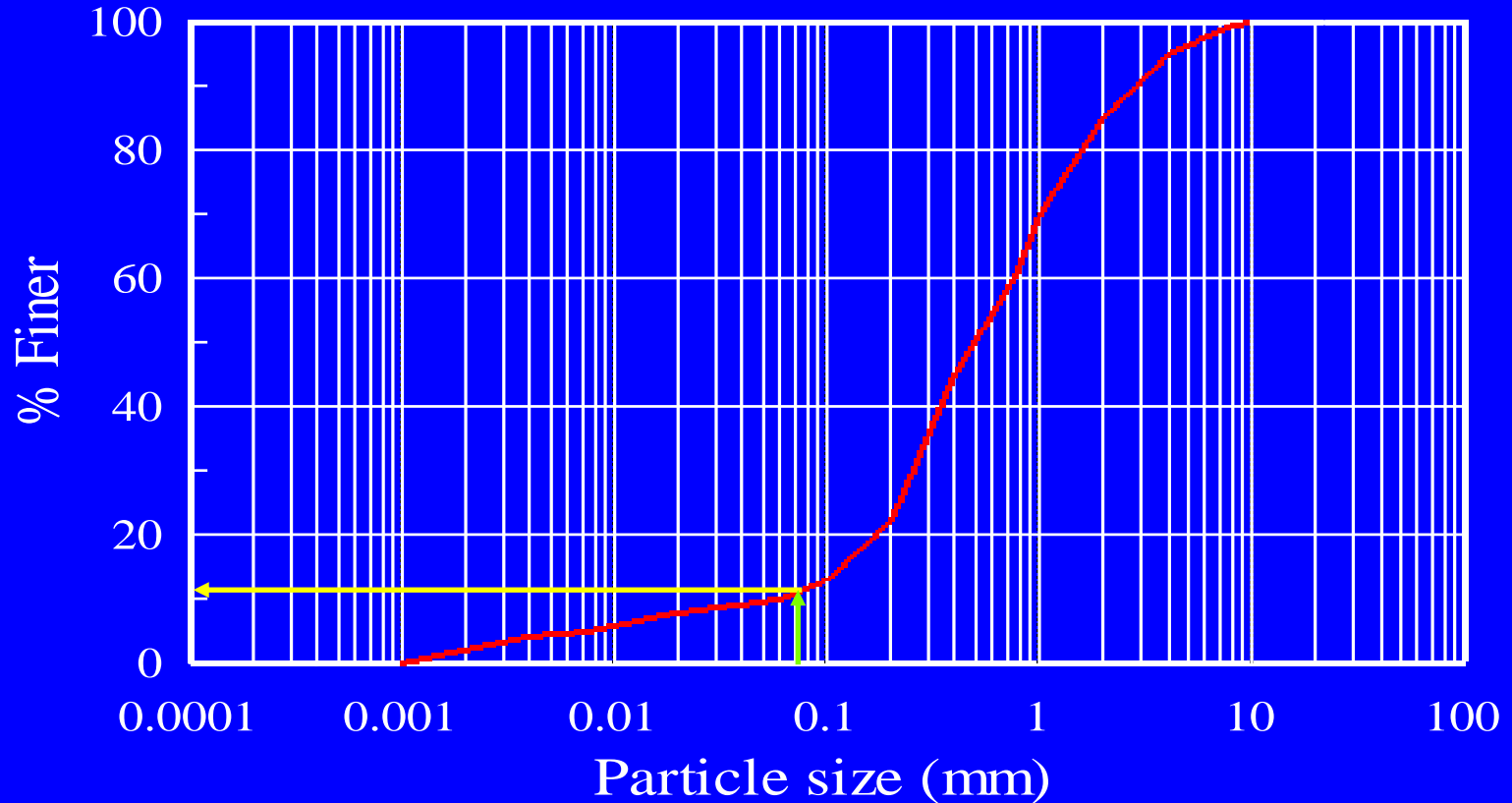
If prefix is G then suffix is W if $C_u > 4$ and C_c is between 1 and 3
otherwise use P

If prefix is S then suffix is W if $C_u > 6$ and C_c is between 1 and 3
otherwise use P

Example

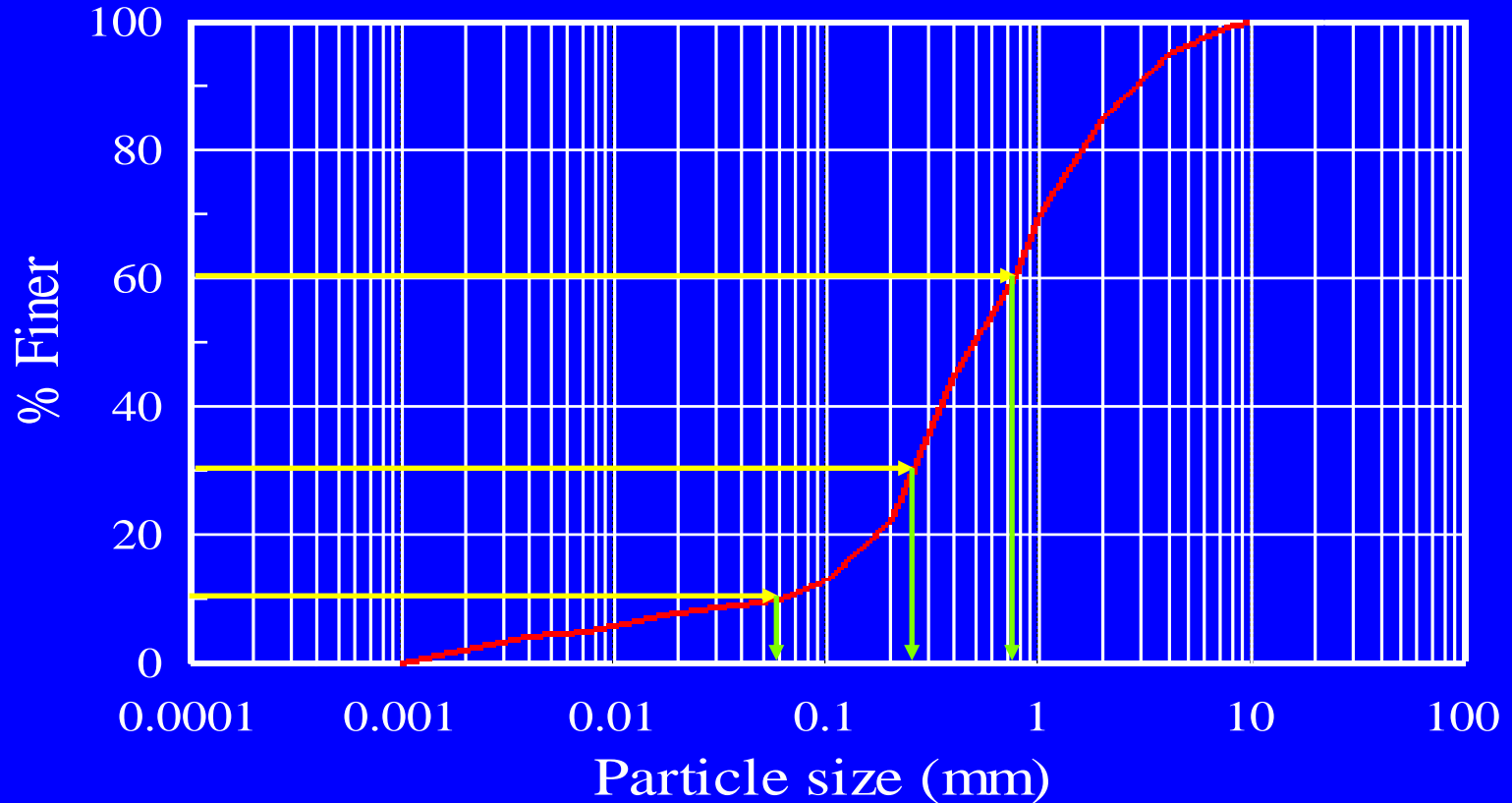


Example



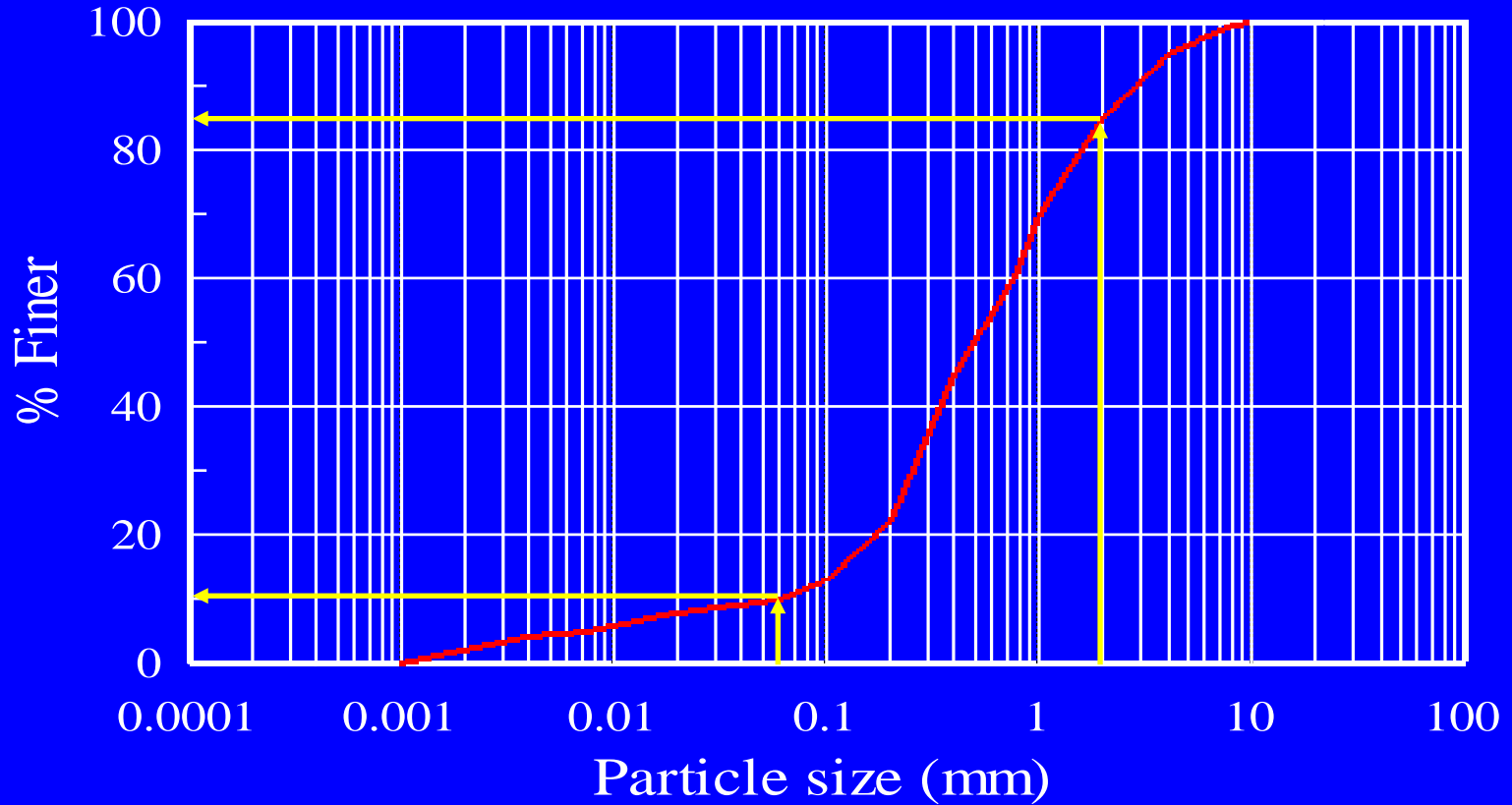
- % fines (% finer than $75 \mu\text{m}$) = 11% - Dual symbols required

Example



- % fines (% finer than $75 \mu\text{m}$) = 11% - Dual symbols required
- $D_{10} = 0.06 \text{ mm}$, $D_{30} = 0.25 \text{ mm}$, $D_{60} = 0.75 \text{ mm}$

Example



Particle size fractions: Gravel 17%
Sand 73%
Silt and Clay 10%

Sieves





Compaction

Purposes of Compaction

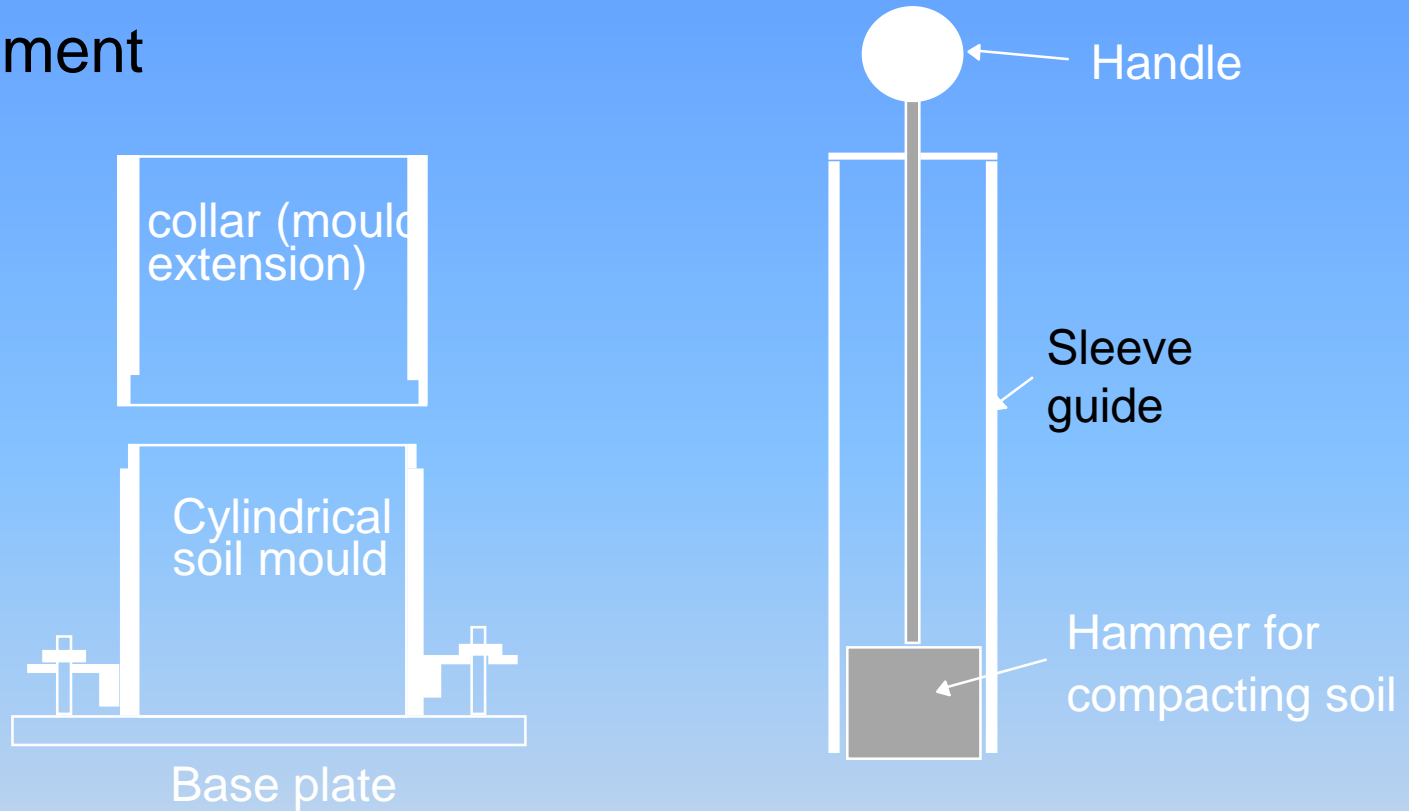
- Compaction is the application of energy to soil to reduce the void ratio
 - This is usually required for fill materials, and is sometimes used for natural soils
- Compaction reduces settlements under working loads
- Compaction increases the soil strength
- Compaction makes water flow through soil more difficult
- Compaction can prevent liquefaction during earthquakes

Factors affecting Compaction

- Water content of soil
- The type of soil being compacted
- The amount of compactive energy used

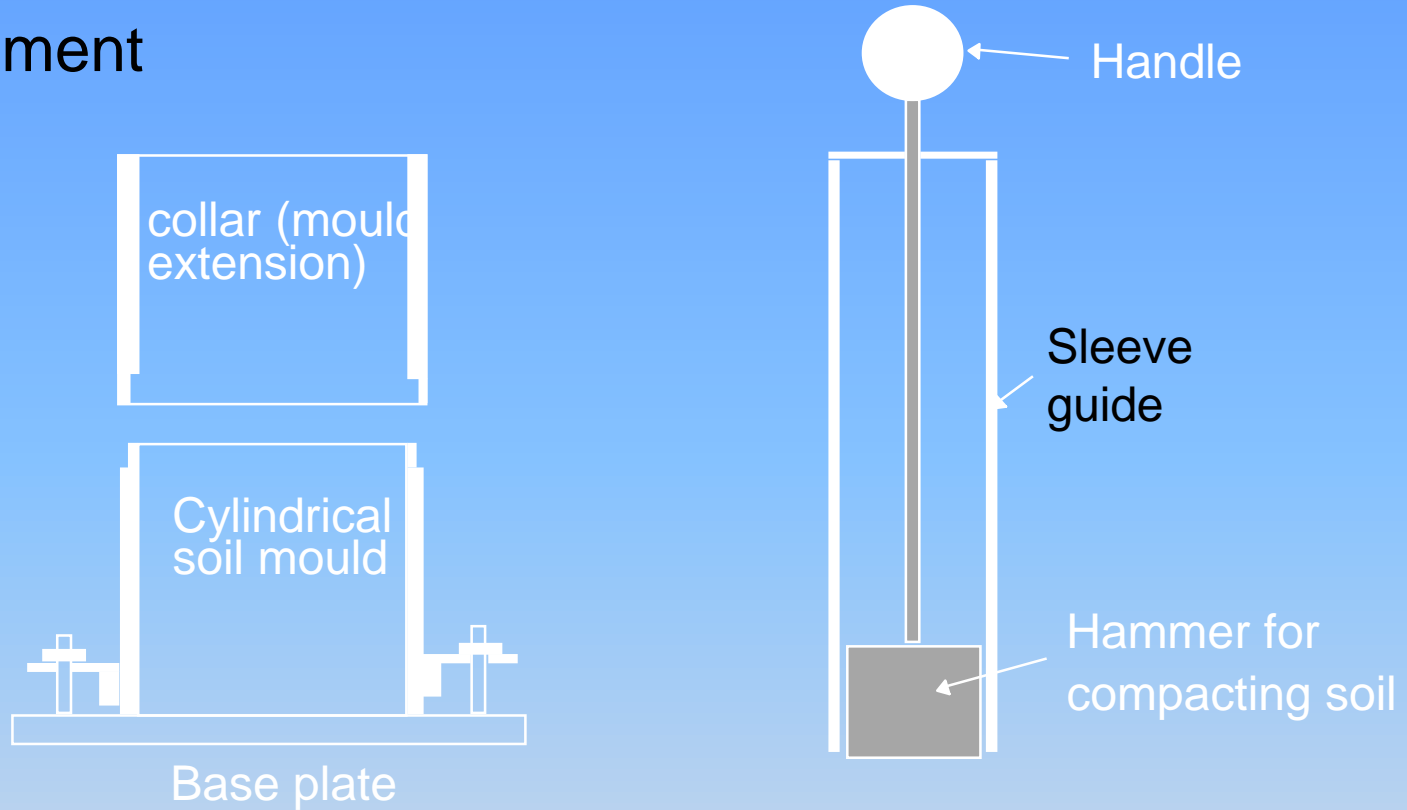
Laboratory Compaction tests

- Equipment



Laboratory Compaction tests

- Equipment



| | Mould volume | Hammer mass | Hammer drop |
|----------|--------------|-------------|-------------|
| Standard | 1000 | 2.5 | 300 |
| Modified | 1000 | 4.9 | 450 |

Presentation of results

- The object of compaction is to reduce the void ratio, or to increase the dry unit weight.

$$\gamma_{dry} = \frac{G_s \gamma_w}{1 + e}$$

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- In a compaction test bulk unit weight and moisture content are measured. The dry unit weight may be determined as follows

$$\gamma_{bulk} = \frac{W}{V} = \frac{\text{Wt of Solids} + \text{Wt of Water}}{\text{Total Volume}} = \frac{W_s + W_w}{V}$$

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$$\gamma_{bulk} = \frac{\left(1 + \frac{W_w}{W_s}\right) W_s}{V}$$

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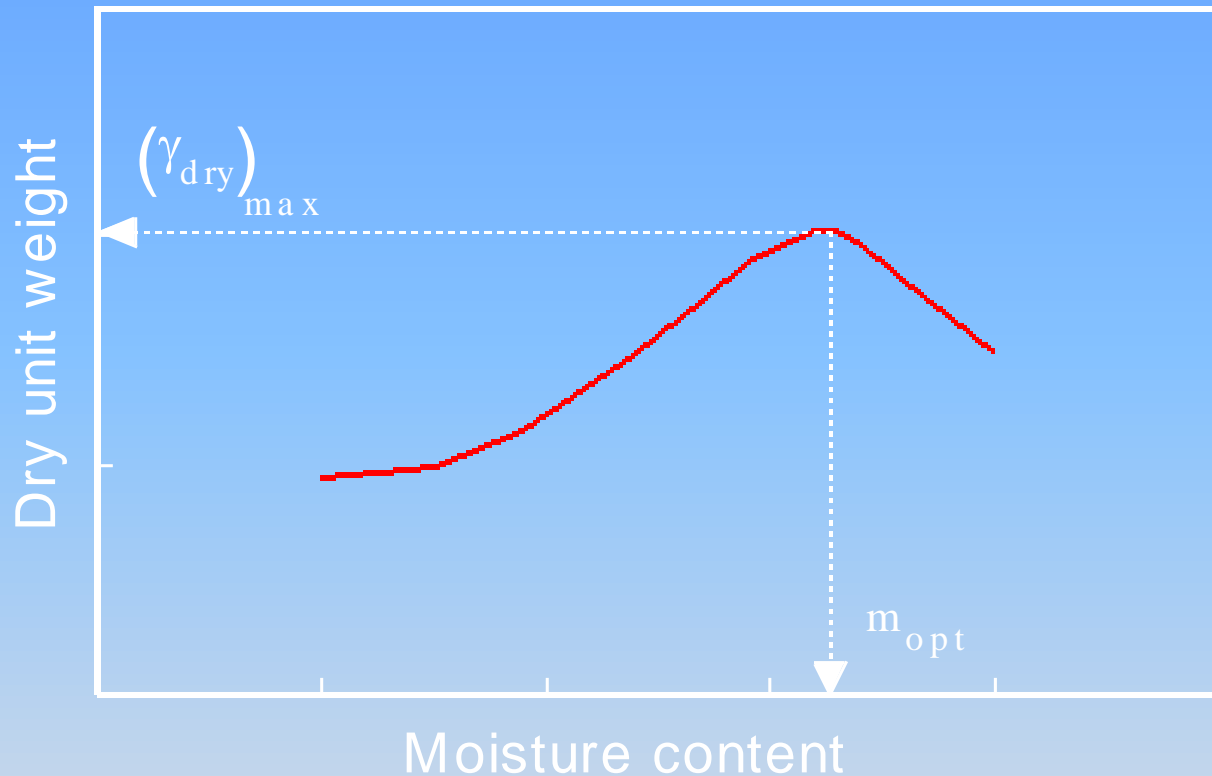
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$$\gamma_{bulk} = \frac{\left(1 + \frac{W_w}{W_s}\right) W_s}{V} = (1 + m) \gamma_{dry}$$

Presentation of Results



From the graph we determine the optimum moisture content, m_{opt} that gives the maximum dry unit weight, $(\gamma_{\text{dry}})_{\text{max}}$.

Presentation of results

- To understand the shape of the curve it is helpful to develop relations between γ_{dry} and the percentage of air voids, A .

$$A (\%) = \frac{V_a}{V} \times 100$$

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$$1 - \frac{A}{100} = \frac{V_w + V_s}{V}$$

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Presentation of results

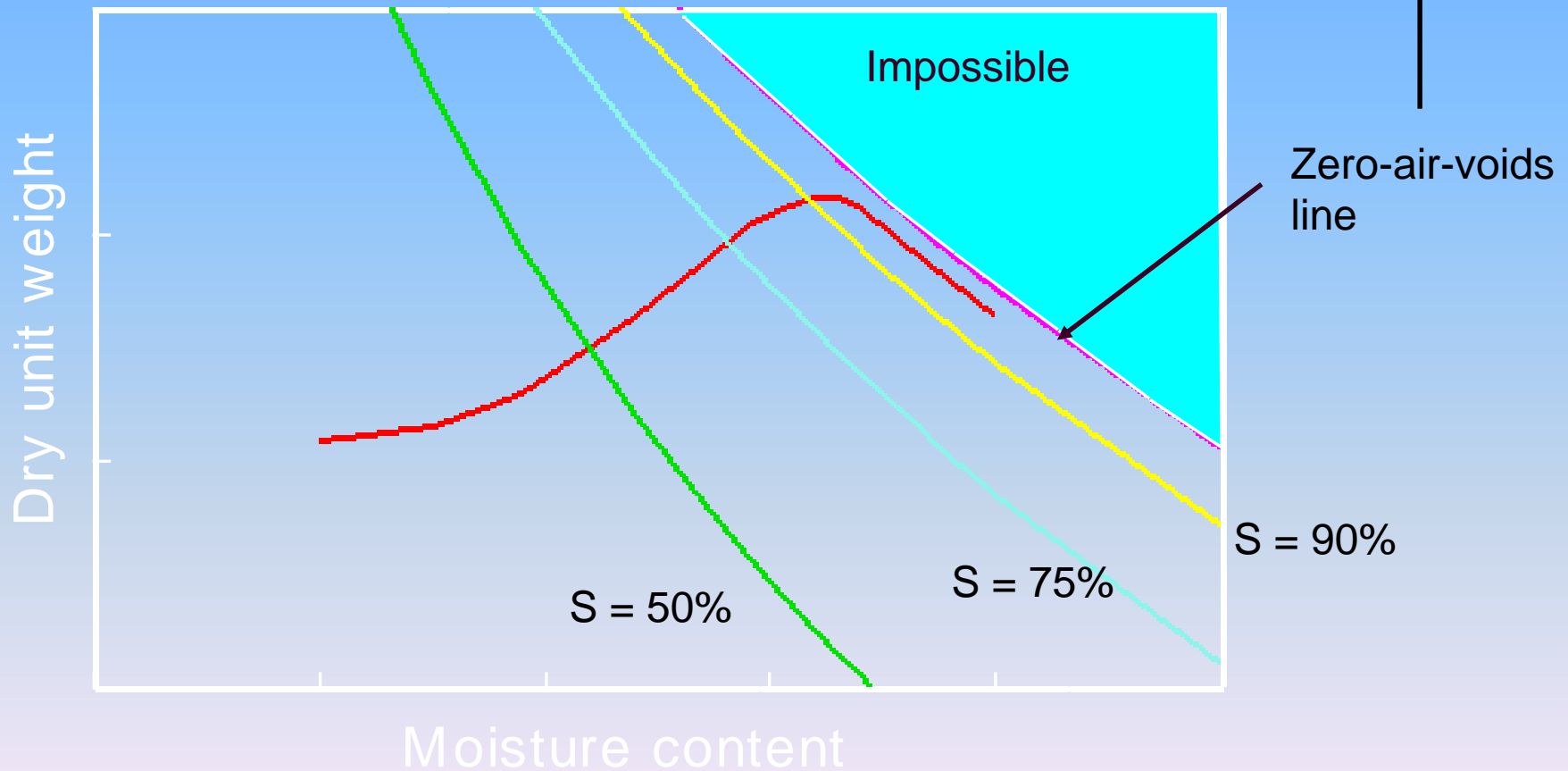
If the soil is saturated ($A = 0$) and

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Presentation of results

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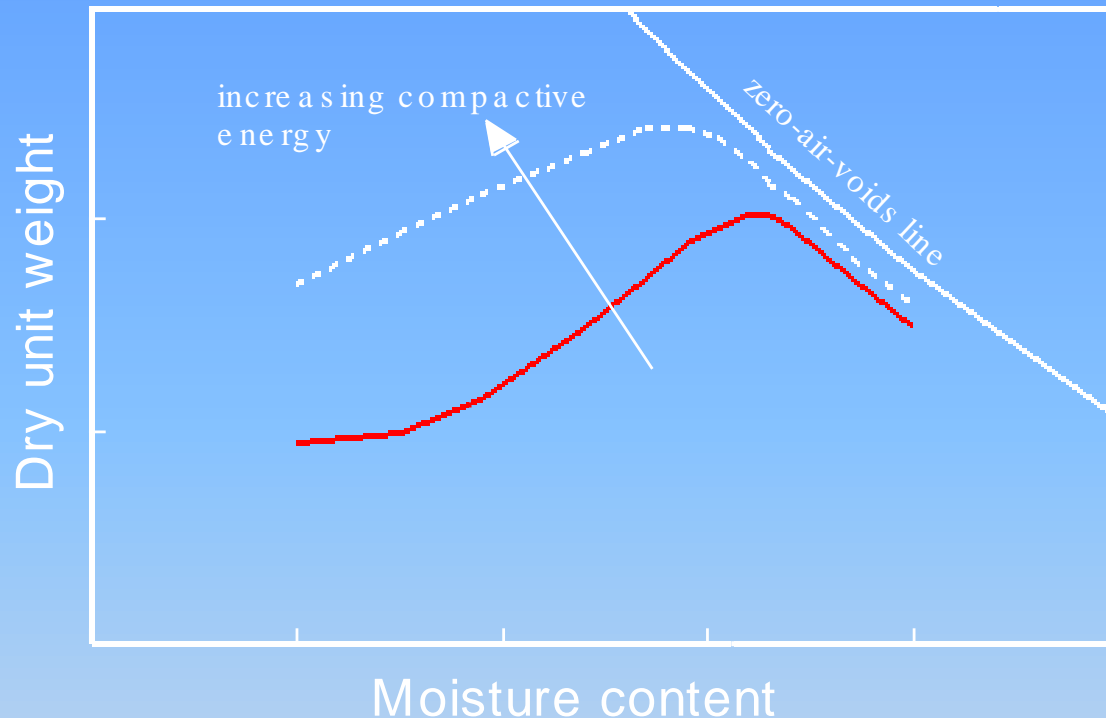
$$\gamma_{dry} = \left[\frac{G_s \gamma_w}{G_s m + 1} \right]$$



Effects of water content

- Adding water at low moisture contents makes it easier for particles to move during compaction, and attain a lower void ratio. As a result increasing moisture content is associated with increasing dry unit weight.
- As moisture content increases, the air content decreases and the soil approaches the zero-air-voids line.
- The soil reaches a maximum dry unit weight at the optimum moisture content
- Because of the shape of the no-air-voids line further increases in moisture content have to result in a reduction in dry unit weight.

Effects of varying compactive effort



- Increasing energy results in an increased maximum dry unit weight at a lower optimum moisture content.
- There is no unique curve. The compaction curve depends on the energy applied.
- Use of more energy beyond m_{opt} has little effect.

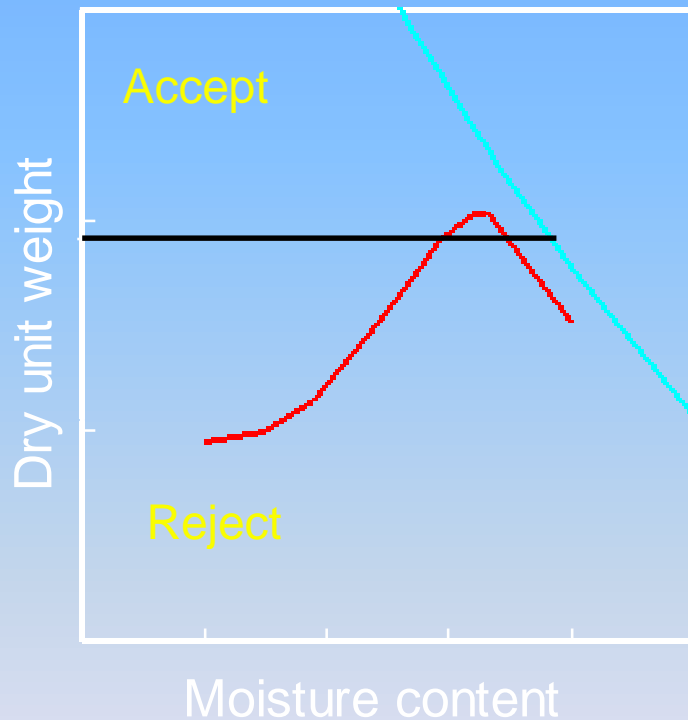
Effects of soil type

| | | Typical Values | |
|----------------------|----|---|----------------------|
| | | $(\gamma_{\text{dry}})_{\text{max}}$ (kN/m ³) | m_{opt} (%) |
| Well graded sand | SW | 22 | 7 |
| Sandy clay | SC | 19 | 12 |
| Poorly graded sand | SP | 18 | 15 |
| Low plasticity clay | CL | 18 | 15 |
| Non plastic silt | ML | 17 | 17 |
| High plasticity clay | CH | 15 | 25 |

- G_s is constant, therefore increasing maximum dry unit weight is associated with decreasing optimum moisture contents
- Do not use typical values for design as soil is highly

Field specifications

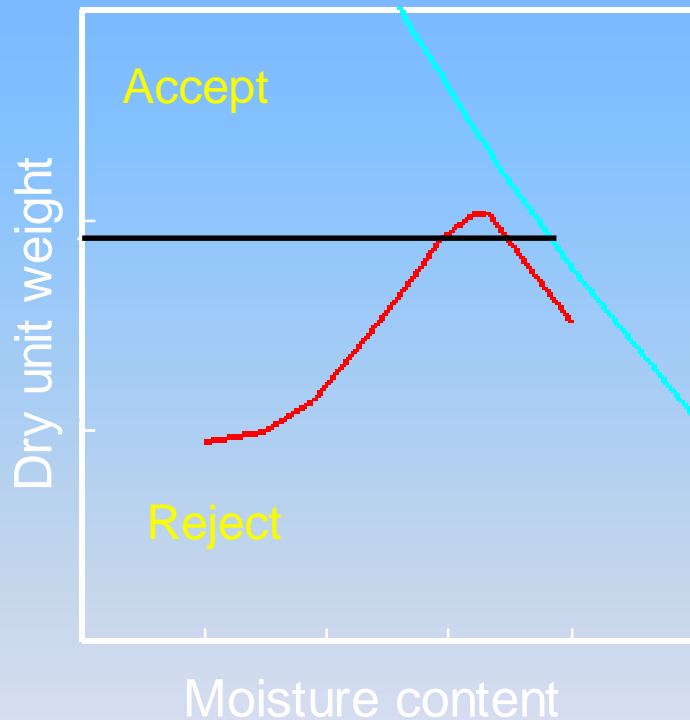
During construction of soil structures (dams, roads) there is usually a requirement to achieve a specified dry unit weight.



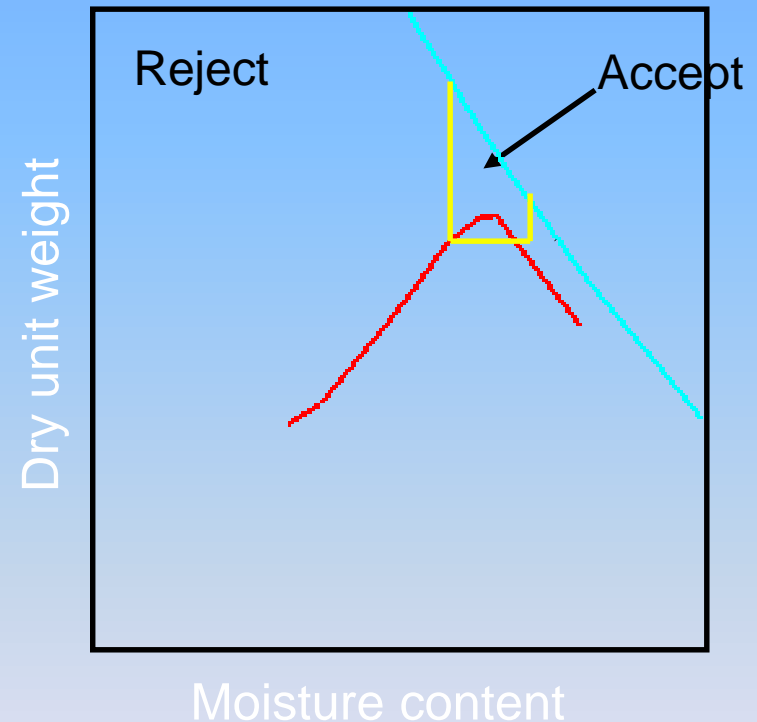
(a) > 95% of (modified)
maximum dry unit weight

Field specifications

During construction of soil structures (dams, roads) there is usually a requirement to achieve a specified dry unit weight.



(a) $> 95\%$ of (modified) maximum dry unit weight



(b) $>95\%$ of (modified) maximum dry unit weight and m within 2% of m_{opt}

Compaction equipment

| Equipment | Most suitable soils |
|---|--|
| Smooth wheeled rollers, static or vibrating | Well graded sand-gravel, crushed rock, asphalt |
| Rubber tired rollers | Coarse grained soils with some fines |
| Grid rollers | Weathered rock, well graded coarse soils |
| Sheepsfoot rollers, static | Fine grained soils with > 20% fines |
| Sheepsfoot rollers, vibratory | as above, but also sand-gravel mixes |
| Vibrating plates | Coarse soils, 4 to 8% fines |
| Tampers, rammers | All types |
| Impact rollers | Most saturated and moist soils |

Also drop weights, vibratory piles







Sands and Gravels

For (cohesionless)soils without fines alternative specifications are often used. These are based on achieving a certain relative density.

$$I_d = \frac{e_{\max} - e}{e_{\max} - e_{\min}}$$

e = current void ratio

e_{\max} = maximum void ratio in a standard test

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$I_d = 1$ when $e = e_{\min}$ and soil is at its densest state

$I_d = 0$ when $e = e_{\max}$ and soil is at its loosest state

Sands and Gravels

We can write I_d in terms of γ_{dry} because we have

$$e = \frac{G_s \gamma_w}{\gamma_{dry}} - 1$$

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The terms loose, medium and dense are used, where typically

loose $0 < I_d < 0.333$

medium $0.333 < I_d < 0.667$

dense $0.667 < I_d < 1$

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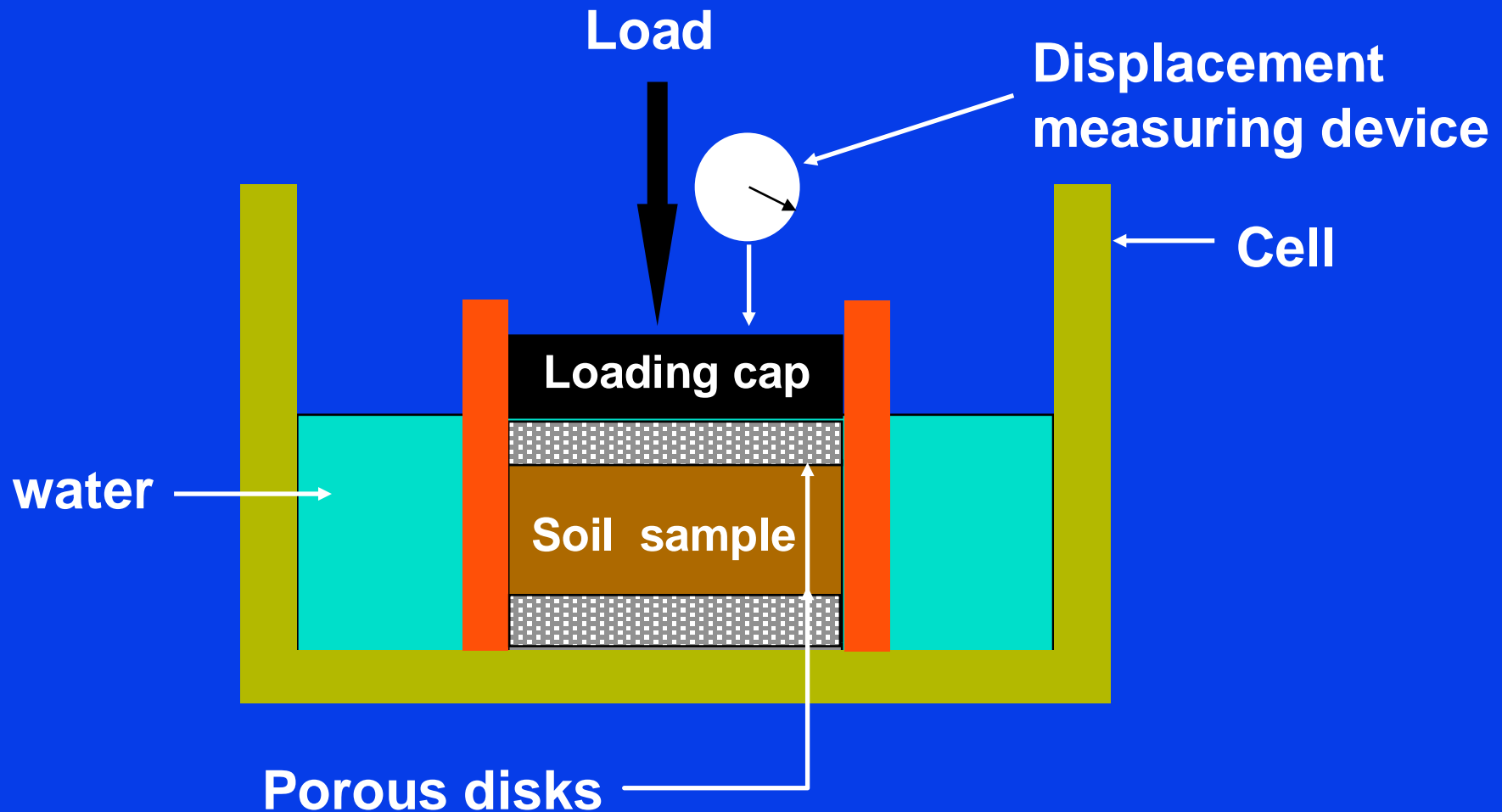
medium $0.333 < I_d < 0.667$

dense $0.667 < I_d < 1$

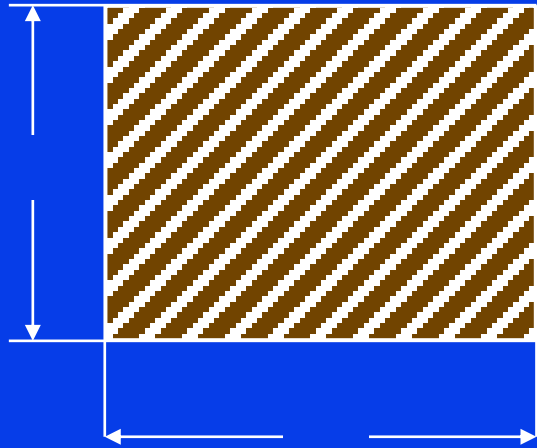
The maximum and minimum dry unit weights vary significantly from soil to soil, and therefore you cannot determine dry unit weight from I_d

Measurement of soil properties

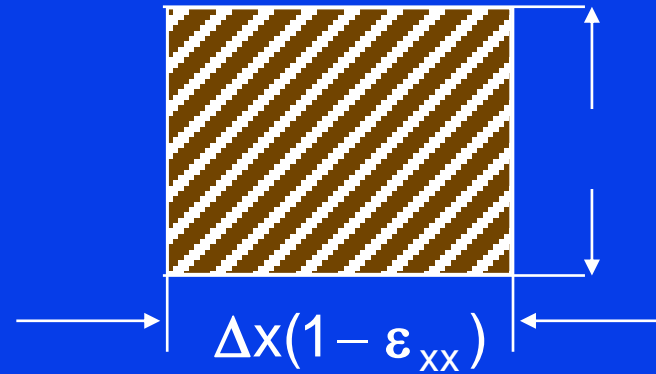
The oedometer apparatus



Relation between axial and volume strain



(a) Before Deformation



(b) After Deformation

$$\text{Volume strain } \epsilon_v = - \frac{\Delta V}{V_0} \quad (1)$$

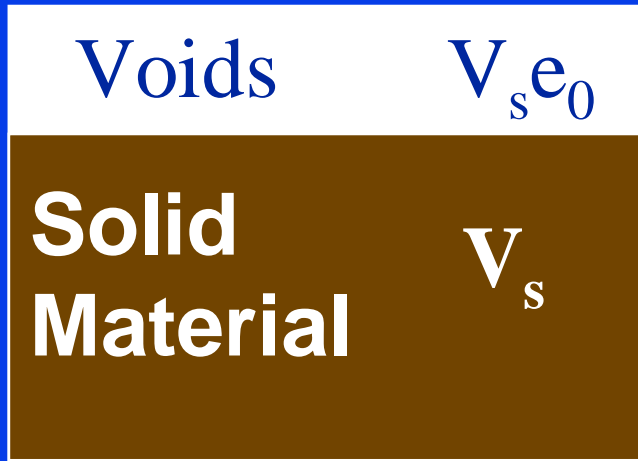
$$(a) \quad V = V_0 = \Delta x \Delta y \Delta z$$

$$(b) \quad V = [\Delta x (1 - \epsilon_{xx})] \times [\Delta y (1 - \epsilon_{yy})] \times [\Delta z (1 - \epsilon_{zz})] \quad (2a)$$

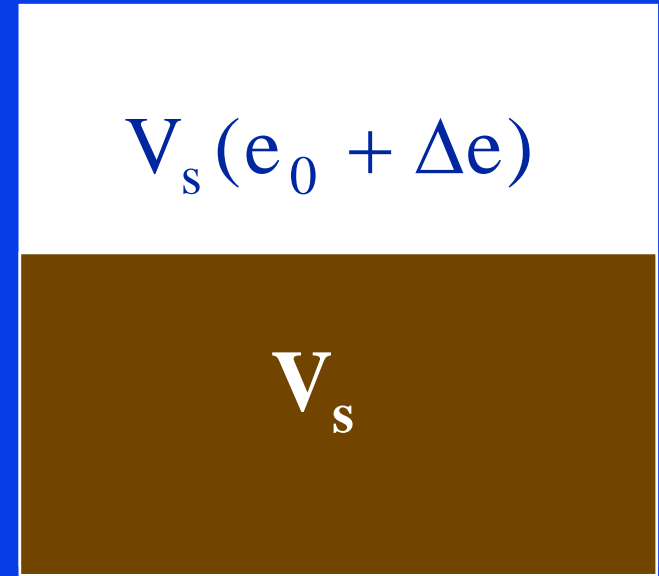
Relation between axial and volume strain

$$\varepsilon_v = - \left(\frac{V - V_0}{V_0} \right) \quad (2b)$$

Relation between volume strain and voids ratio



(a) Before Deformation

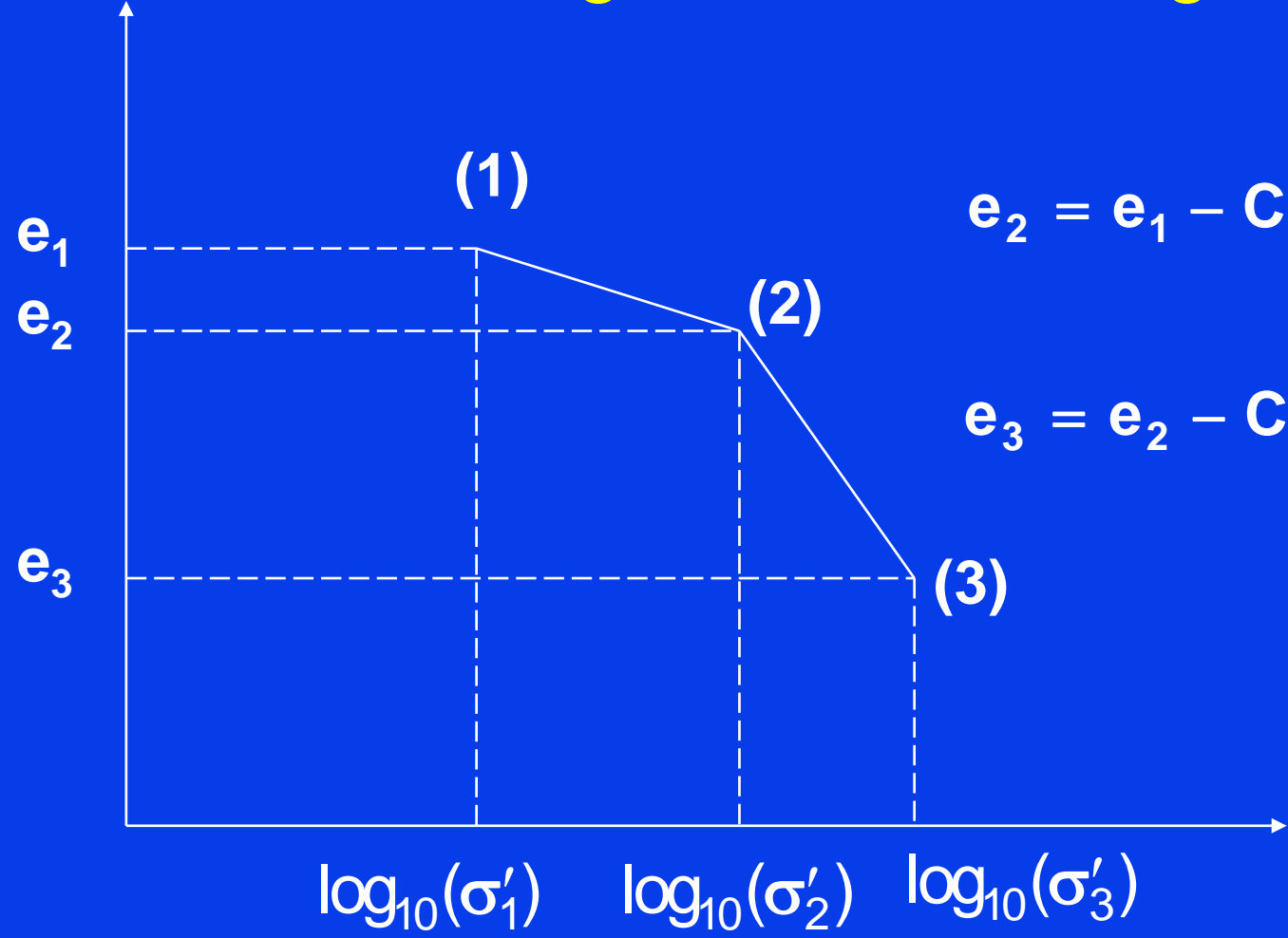


(b) After Deformation

$$V_0 = V_s (1 + e_0)$$

$$V = V_s (1 + e_0 + \Delta e)$$

Voids ratio change for soil moving from OC to NC

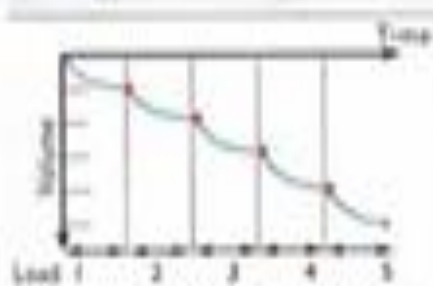
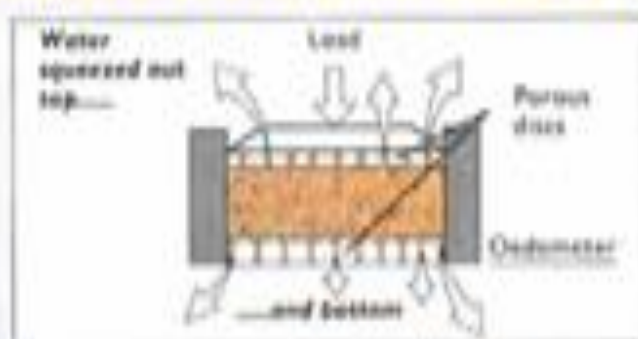


$$e_2 = e_1 - C_r \log_{10} \left(\frac{\sigma'_2}{\sigma'_1} \right) \quad (8a)$$

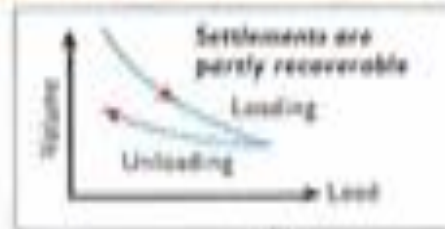
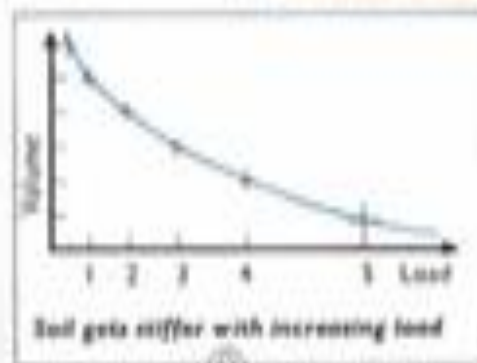
$$e_3 = e_2 - C_c \log_{10} \left(\frac{\sigma'_3}{\sigma'_2} \right) \quad (8b)$$

The initial value of $\sigma'_{pc} = \sigma'_2$
The final value of $\sigma'_{pc} = \sigma'_3$

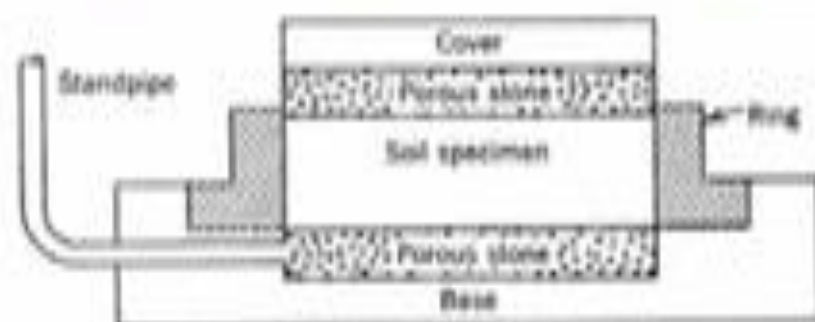
Consolidation Apparatus ("oedometer")



Consolidation is time dependent:
coarse grain soil = fast
fine grained soil = slow



ELE catalogue



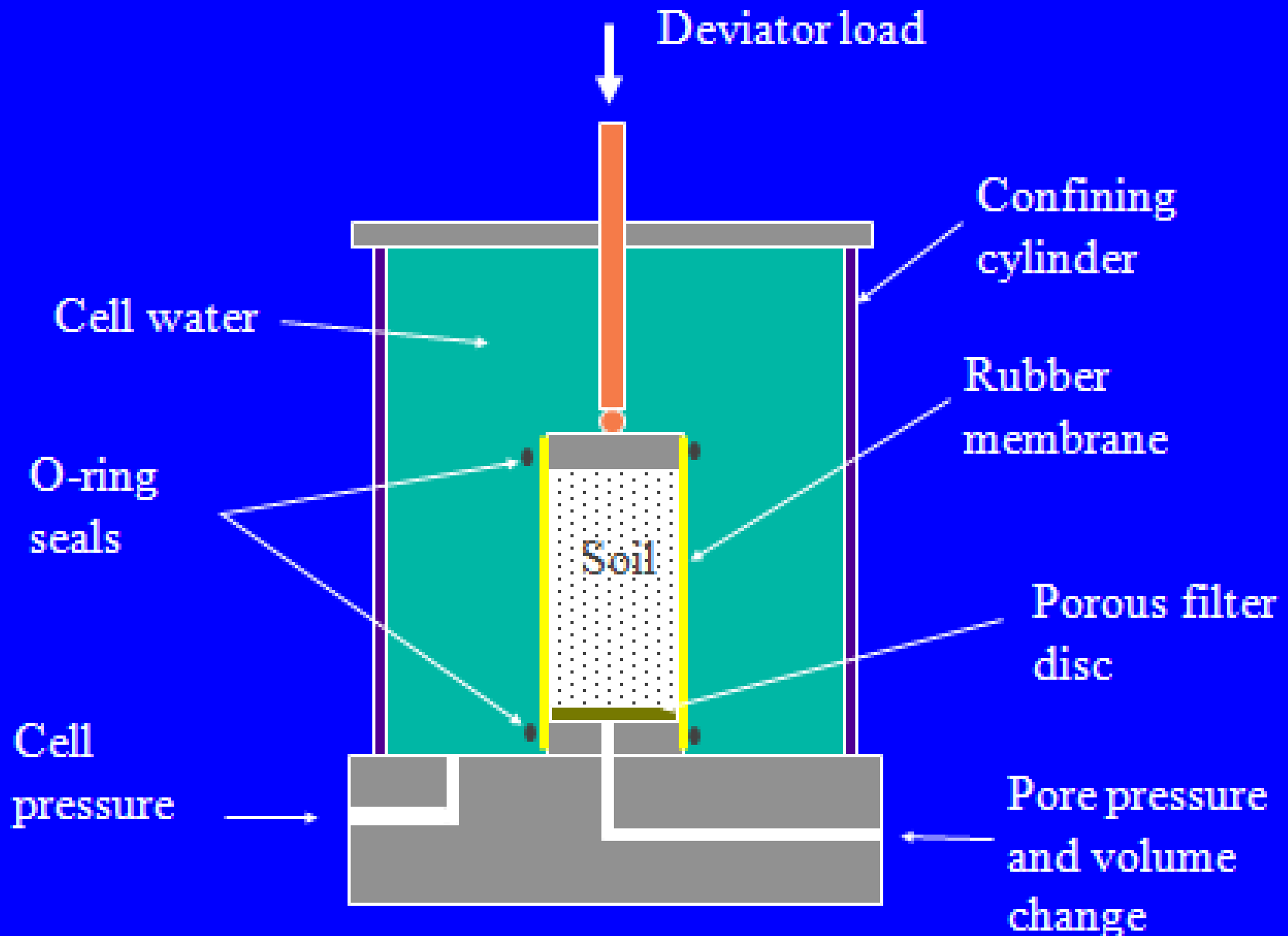
Oedometers

Unconfined compression test on clay (undrained, uniaxial)



Tests to measure soil strength

2. The Triaxial Test



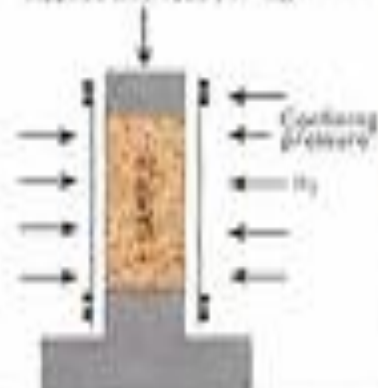


Triaxial Test on Soil Sample in Laboratory

Total Stress Measurement

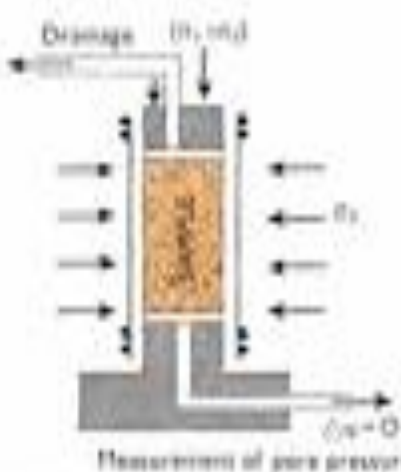
Quick Undrained (QU) and
Unconsolidated Undrained (UU)

Applied axial load ($\sigma_1 - \sigma_3$)

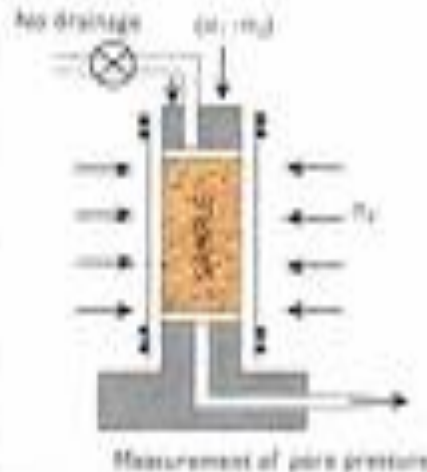


Effective Stress Measurement

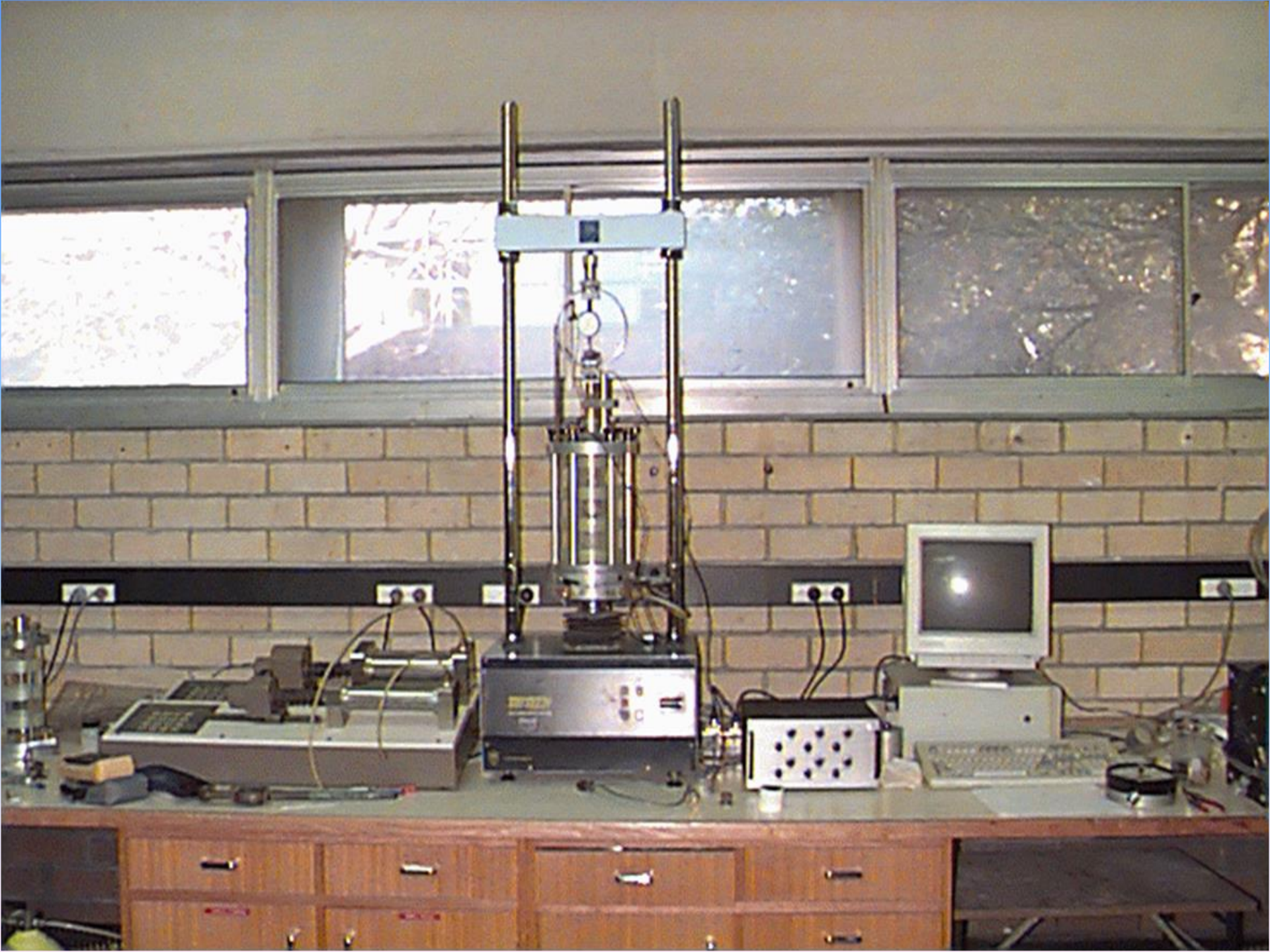
Consolidation Drained (CD)



Consolidation Undrained (CU)



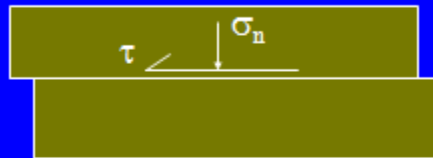
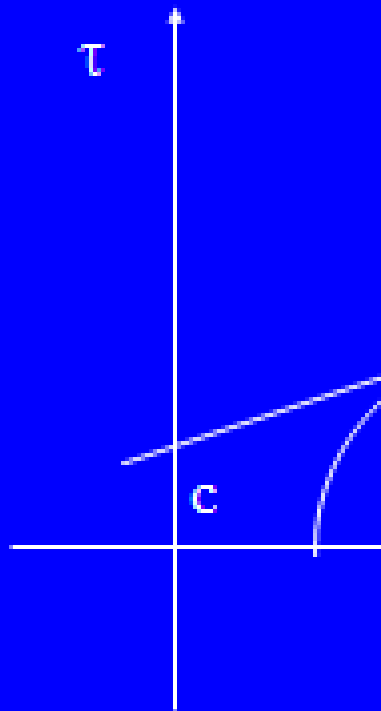
Triaxial test on soil



Mohr Circles

To relate strengths from different tests we need to use some results from the Mohr circle transformation of stress.

Mohr-Coulomb failure criterion



$$+ \sigma \tan \phi$$

The limiting shear stress (soil strength) is given by

$$\tau = c + \sigma_n \tan \phi$$

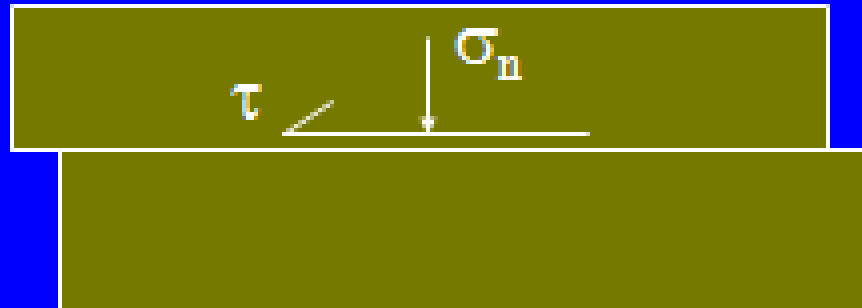
where c = cohesion (apparent)

ϕ = friction angle

—————→ σ

The Mohr-Coulomb failure locus is tangent to the Mohr circles at failure

Mohr-Coulomb failure criterion



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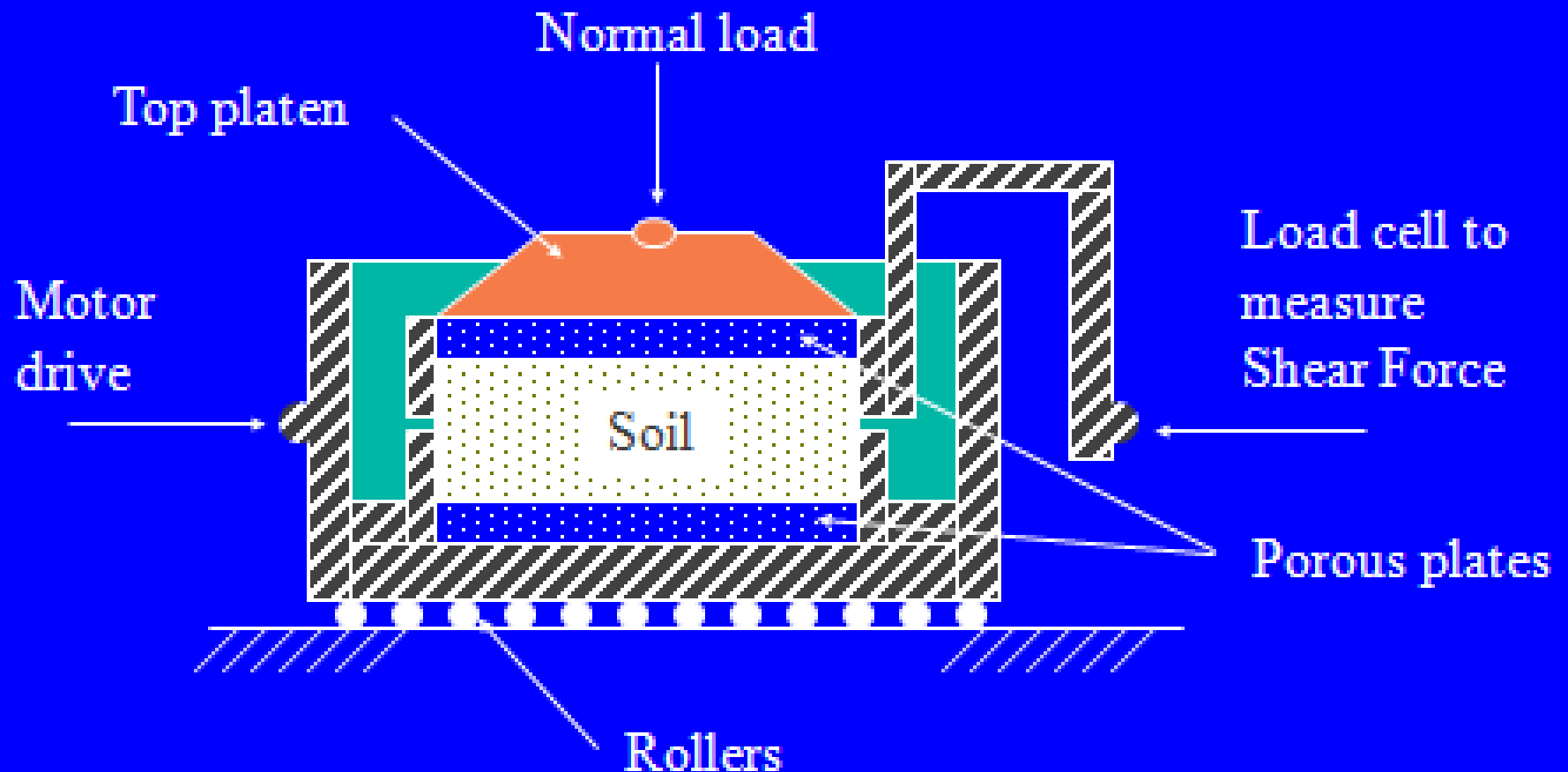
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Tests to measure soil strength

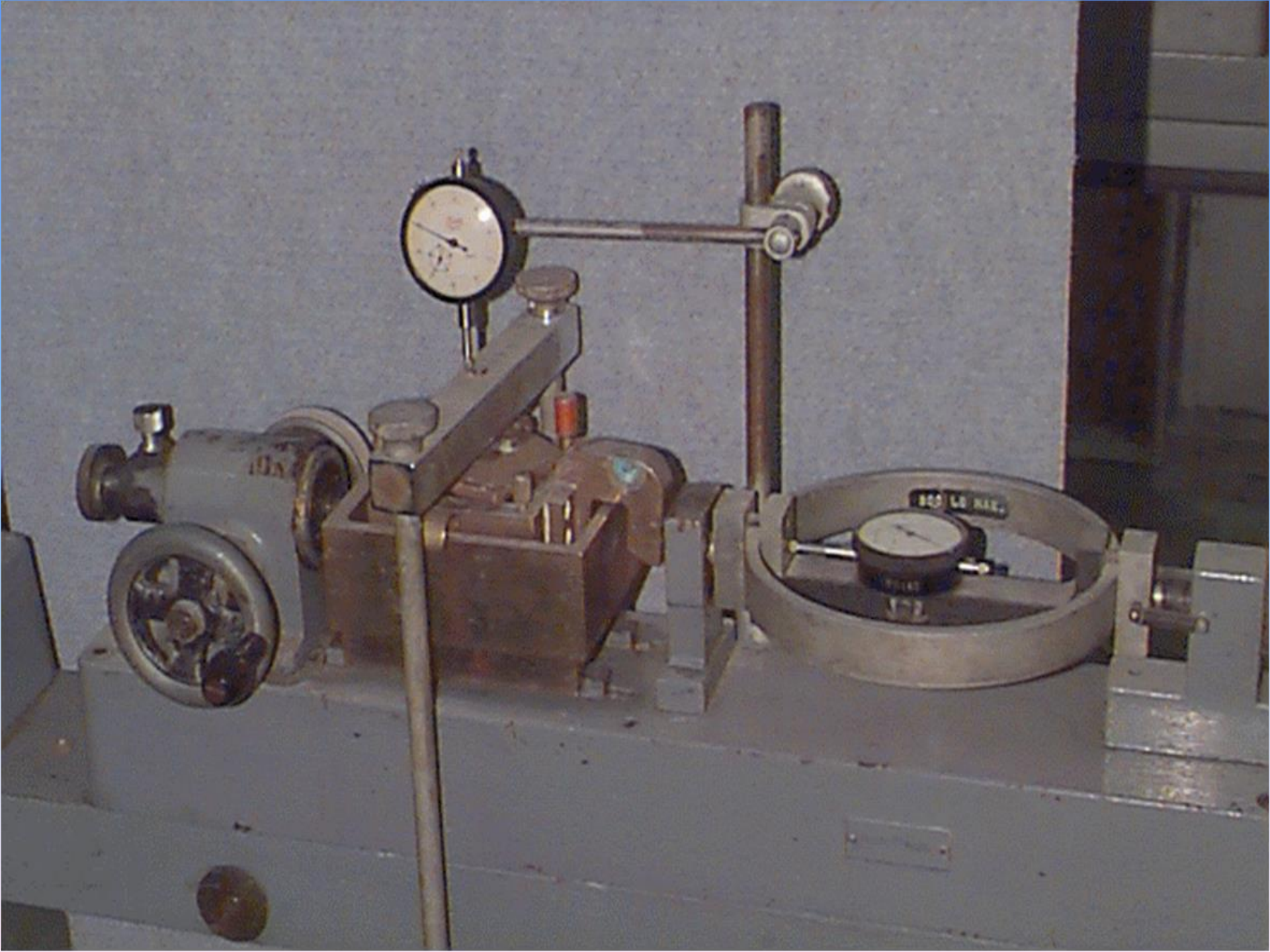
1. Shear Box Test

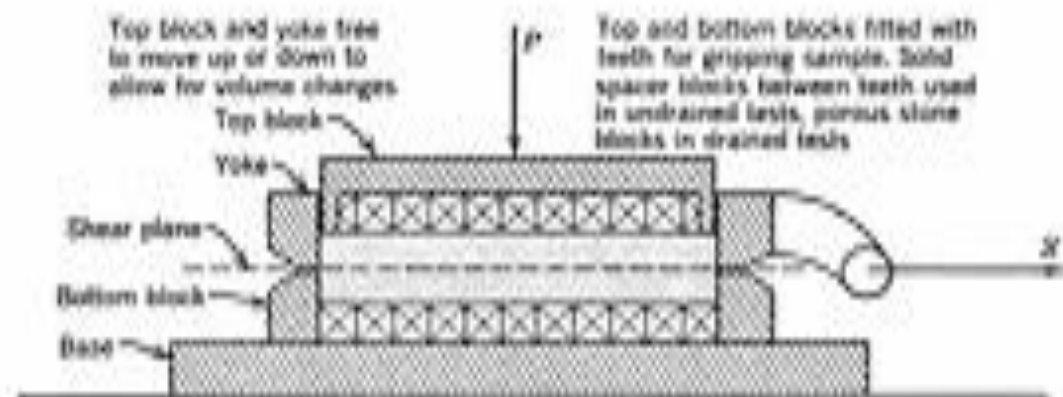


Measure

relative horizontal displacement, dx

vertical displacement of top platen, dy





Direct shear (shear box) test on soil

Shear box test

- ◆ Usually only relatively slow drained tests are performed in shear box apparatus. For clays rate of shearing must be chosen to prevent excess pore pressures building up. For sands and gravels tests can be performed quickly
- ◆ Tests on sands and gravels are usually performed dry. Water does not significantly affect the (drained) strength.
- ◆ If there are no excess pore pressures and as the pore pressure is approximately zero the total and effective stresses will be identical.
- ◆ The failure stresses thus define an effective stress failure envelope from which the effective (drained) strength parameters c' , ϕ' can be determined.